BIOPHYSICS LETTER



On the use of one-step perturbation to investigate the dependence of NOE-derived atom-atom distance bound violations of peptides upon a variation of force-field parameters

Zhixiong Lin · Chris Oostenbrink · Wilfred F. van Gunsteren

Received: 23 October 2013 / Revised: 13 January 2014 / Accepted: 17 January 2014 / Published online: 7 February 2014 © European Biophysical Societies' Association 2014

Abstract The method of one-step perturbation can be used to predict from a single molecular dynamics simulation the values of observable quantities as functions of variations in the parameters of the Hamiltonian or biomolecular force field used in the simulation. The method is used to predict violations of nuclear overhauser effect (NOE) distance bounds measured in nuclear magnetic resonance (NMR) experiments by atom-atom distances of the NOE atom pairs when varying force-field parameters. Predictions of NOE distance bound violations between different versions of the GROMOS force field for a hexa- β -peptide in solution show that the technique works for rather large force-field parameter changes as well as for very different NOE bound violation patterns. The effect of changing individual force-field parameters on the NOE distance bound violations of the β -peptide and an α -peptide was investigated too. One-step perturbation, which in this case is equivalent to reweighting configurations, constitutes an efficient technique to predict many values of different quantities from a single conformational ensemble for a particular system, which makes it a powerful force-field development technique that easily reduces the number of required separate simulations by an order of magnitude.

Z. Lin · W. F. van Gunsteren (⊠) Laboratory of Physical Chemistry, Swiss Federal Institute of Technology, ETH, 8093 Zurich, Switzerland e-mail: wfvgn@igc.phys.chem.ethz.ch

C. Oostenbrink

Institute for Molecular Modeling and Simulation, University of Natural Resources and Life Sciences (BOKU), Vienna, Austria Keywords Molecular dynamics (MD) simulation \cdot One-step perturbation \cdot Reweighting \cdot NOE distance bound violations \cdot Peptide

Molecular dynamics (MD) simulation represents a useful tool for investigating the properties of molecular systems relevant in physics, chemistry, and biology. However, the quality of the results obtained from MD simulations depends on the extent of sampling of the conformational space accessible to a molecular system and on the accuracy of the underlying force field (van Gunsteren and Berendsen 1990). A major effort in the realm of molecular simulation is thus directed towards the parametrization and validation of force fields against available experimental data (Cornell et al. 1995; Jorgensen et al. 1996; MacKerell et al. 1998; Reif et al. 2012).

The parametrization philosophy of the GROMOS force field (van Gunsteren et al. 2006; van Gunsteren et al. http://www.gromos.net) is to determine as many values of the parameters as possible by fitting particular properties of small molecules in the condensed phase as simulated to corresponding experimental values (Horta et al. 2011), and to subsequently validate the force field against experimental data of biomolecular systems such as peptides, proteins, nucleic acids, carbohydrates, and lipids. To avoid jeopardizing the transferability of parameters between groups of atoms in different molecules, data on large molecules are not used in the parametrization phase. If one were to use such data from molecules such as proteins, e.g., structures from the Protein Data Bank, properties of groups of atoms may well be dependent on their particular environment in the folded molecule. Furthermore, the Protein Data Bank contains structures derived from measurements at different thermodynamic conditions of pH, ionic strength, etc. Using the GROMOS force field, generally, good agreement with experimental data of biomolecules was obtained; see, for example, a recent validation of the new GROMOS 54A8 force field (Reif et al. 2013). However, in case experimental data for test molecules are not reproduced, e.g., the conformational preference of a hexa- β -peptide in solution was shown to be wrongly described by the GROMOS 54A7 force field (Lin and van Gunsteren 2013), the responsible force-field parameter is to be identified. This could be done by running additional simulations with different values of force-field parameters and different combinations thereof, which is, however, computationally very costly. In this communication, we illustrate a technique that can give an indication of which force-field parameters should be changed without the need of repeating simulations.

One-step perturbation (Liu et al. 1996) is an efficient method to calculate many free energy differences from a single simulation (Oostenbrink 2012). It can, however, also be applied to predict structural properties from a single simulation (Oostenbrink and van Gunsteren 2005; Hritz and Oostenbrink 2009; Li and Brüschweiler 2010; Bachmann et al. 2013). Examples are the occurrence of hydrogen bonds (Oostenbrink and van Gunsteren 2005), NMR ³J-coupling constants (Hritz and Oostenbrink 2009), and properties of liquid water (Bachmann et al. 2013). The same idea was also applied to optimize the Amber ff99SB force field with respect to chemical shifts of proteins (Li and Brüschweiler 2010).

Using one-step perturbation, structural properties can be predicted as follows. For a quantity $Q(\vec{r}^N)$ that depends on the coordinates $\vec{r}^N = (\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)$ of a system of Nparticles, the average $\langle Q \rangle_A$ of the quantity $Q(\vec{r}^N)$ calculated over the ensemble of configurations \vec{r}^N generated using the Hamiltonian H_A can be predicted from a reference simulation of the reference Hamiltonian H_R ,

$$\langle Q \rangle_{\rm A} = \frac{\left\langle Q e^{-(H_{\rm A} - H_{\rm R})/k_{\rm B}T} \right\rangle_{\rm R}}{\left\langle e^{-(H_{\rm A} - H_{\rm R})/k_{\rm B}T} \right\rangle_{\rm R}},\tag{1}$$

in which $\langle \cdots \rangle_{\rm R}$ denotes the ensemble average over the configurations sampled in the reference simulation. In this way, the quantity $\langle Q \rangle_{\rm A}$ for many different Hamiltonians $H_{\rm A}$ can be predicted from a single simulation using the reference Hamiltonian $H_{\rm R}$. This application of one-step perturbation consists of reweighting the configurations \vec{r}^N of the ensemble R with the factor ${\rm e}^{-(H_{\rm A}(\vec{r}^N)-H_{\rm R}(\vec{r}^N))/k_{\rm B}T}/\sum {\rm e}^{-(H_{\rm A}(\vec{r}^N)-H_{\rm R}(\vec{r}^N))/k_{\rm B}T}$ and is similar to the unbiasing step in umbrella sampling (Torrie and Valleau 1977).

The accuracy of Eq. (1) in predicting structural properties depends on the overlap of the configurations belonging to H_A and H_R , and on the accuracy of the function $Q(\vec{r}^N)$ that connects the observable Q to a configuration \vec{r}^N . Regarding the latter, the relation between a chemical shift and a molecular structure is not completely understood, and the Karplus relation ${}^{3}J(\theta)$ relating a ${}^{3}J$ -coupling constant to a torsional angle θ has a large statistical uncertainty (Steiner et al. 2012). On the other hand, a NOE intensity is related to the atom–atom distance r_{ij} of the atoms *i* and *j* involved in the NOE,

$$Q(r_{ij}) \propto r_{ij}^{-6}.$$
 (2)

So, this quantity Q will be used in this study. For a protein, the set of NOE atom-atom distances may not be very sensitive to changes in force-field parameters as long as the particular fold of the protein is maintained (Eichenberger et al. 2010). For small flexible peptides though, different conformations may be present in the ensemble and may contribute to $\langle Q \rangle_A$, and the relative occurrence of the different conformations is generally sensitive to force-field parameter changes.

Based on the above considerations, we use one-step perturbation or reweighting to predict the NOE distance bound violations for a hexa- β -peptide (Seebach et al. 1998; Daura et al. 1999) (H₂⁺- β ²-HVal- β ³-HAla- β ²-HLeu- β ³-HVal- β ²-HAla- β ³-HLeu-OH) and a hepta- α -peptide (Seebach et al. 2005; Wang et al. 2010) (Val-Ala-Leu-Aib-Ile-Met-Phe). The accuracy of the technique is first tested through perturbations between different GROMOS force fields for the β -peptide. Next, the method is used to predict the effect of changing individual force-field parameters on the NOE distance bound violations of both peptides.

The simulations of the two peptides were carried out in explicit methanol solvent using the GROMOS11 simulation package (van Gunsteren et al. http://www.gromos.net; Eichenberger et al. 2011; Riniker et al. 2011; Schmid et al. 2011a, 2012). The simulation temperatures and lengths are listed in Table 1. The details of the simulation setup are described by Lin and van Gunsteren (2013) for the β -peptide and Wang et al. (2010) for the α -peptide. Interproton distance bounds derived from the NOE cross-peak

Table 1 Overview of the MD simulations

Peptide	Simulation name	Force field ^a	No. solvent molecules	<i>T</i> (K)	Simulation time (ns)
Ρβ	Ρβ_45Α3	45A3	1,123	340	500
	<i>Pβ_53A6*</i> ^b	_	1,123	340	500
	<i>Pβ_53A6</i>	53A6	1,123	340	500
	<i>Pβ_54A7</i>	54A7	1,123	340	500
Ρα	<i>Ρα_53Α6</i>	53A6	1,556	300	200

^a GROMOS force fields used for the peptides: 45A3 (Schuler et al. 2001), 53A6 (Oostenbrink et al. 2004), 54A7 (Schmid et al. 2011b)

 b The 53A6 force field was used for the $\beta\text{-peptide},$ and 45A3 for the methanol solvent

intensities (Seebach et al. 1998, 2005) were compared with the corresponding average effective interproton distances in the simulations, calculated as $\langle r^{-6} \rangle^{-1/6}$. The hydrogen– hydrogen distances involving aliphatic hydrogen atoms were calculated by defining virtual (CH₁), prochiral (stereospecific CH₂), and pseudo (CH₃ and nonstereospecific CH₂) atomic positions, and the distance bounds for the latter were modified to include pseudo-atom distance bound corrections (0.10 nm for nonstereospecific CH₂, 0.15 nm for CH₃, and 0.29 nm for nonstereospecific rotating methvls) (Wüthrich et al. 1983).

The NOE distance bound violations out of the 32 NOE distance bounds (Seebach et al. 1998) of the β -peptide using different GROMOS force fields are shown in Fig. 1a, d, and g for GROMOS 45A3, 53A6, and 54A7, respectively. The 45A3 (Schuler et al. 2001) and 53A6 (Oostenbrink et al. 2004) force fields have sizable differences in their parameter values of the backbone atom partial charges (up to 20 %), terminal group partial charges (up to 50 %), as well as the van der Waals parameters of the polar backbone atoms (up to 20 %), yet the simulations



of the β -peptide using these two force fields show a very

similar picture of NOE bound violations; i.e., for both force fields, there are six positive violations <0.1 nm for the same hydrogen-hydrogen distances (Lin and van Gunsteren 2013). In contrast, the 54A7 force field (Schmid et al. 2011b) gives a completely different violation pattern with five positive NOE bound violations larger than 0.1 nm (Lin and van Gunsteren 2013), although it only differs from 53A6 (Oostenbrink et al. 2004) in the backbone φ and ψ torsional angle energy terms and the backbone N and O van der Waals interactions for this β -peptide.

Figure 2 shows a comparison of NOE bound violations of the β -peptide predicted by one-step perturbation and evaluated from direct MD simulations. Since 45A3 has a different solvent methanol model, an additional simulation was carried out with 53A6 as the solute force field, and 45A3 as the methanol solvent force field (Table 1). This allows for determination of the effect of changing only the solute force-field parameters. According to Fig. 2, the prediction by one-step perturbation is very accurate; i.e., the deviations between the predicted violations and the simulated ones are mostly within 0.02 nm. The accurate prediction when perturbing from 45A3 to 53A6 shows that the technique works for rather large force-field parameter changes, and the perturbation between 53A6 and 54A7 illustrates that the technique works for very different NOE bound violation patterns. We note in passing that the 53A6 force field (blue and green symbols in Fig. 2) yields much



Fig. 2 Comparison of NOE atom-atom distance bound violations of the β -peptide predicted by one-step perturbation and evaluated from MD simulation. Blue plus sign NOE violations predicted by $P\beta_45A3$ compared with the ones evaluated from $P\beta_{53A6*}$; red cross NOE violations predicted by $P\beta_{-}53A6$ compared with the ones evaluated from $P\beta$ 54A7; green circle NOE violations predicted by $P\beta$ 54A7 compared with the ones evaluated from $P\beta_53A6$. The dashed lines indicate a deviation of 0.02 nm. The hydrogen atom pairs with violations larger than 0.1 nm are listed. H*-C^{β} refers to nonstereospecific protons bound to C^f

Fig. 1 Comparison of r^{-6} averaged NOE distances as obtained from simulations or predicted by one-step perturbation and experimental data for $P\beta$. **a** $P\beta_45A3$; **b** 53A6 predicted by $P\beta_45A3$; **c** 54A7 predicted by $P\beta_{45A3}$; **d** $P\beta_{53A6}$; **e** 45A3 predicted by $P\beta_{53A6}$; **f** 54A7 predicted by $P\beta_{53A6}$; **g** $P\beta_{54A7}$; **h** 45A3 predicted by $P\beta_{54A7}$; i 53A6 predicted by $P\beta_{54A7}$

Fig. 3 Sum of the positive NOE distance bound violations for the β -peptide predicted by one-step perturbation using the $P\beta_{-}53A6$ simulation as the reference state and varying different force-field parameters



smaller violations than the 54A7 one (red symbols in Fig. 2).

In a previous study, Bachmann et al. (2013) concluded that one-step perturbation can only be used to qualitatively predict different properties of liquid water. In contrast, the NOE distance bound violations of the β -peptide can be predicted using one-step perturbation not only qualitatively, but also quantitatively. The less accurate prediction in the previous study is related to the larger size of the perturbation considered in that study, i.e., changing force-field parameters by 5 % for up to 5,000 water molecules (Bachmann et al. 2013).

Next, one-step perturbation was used to investigate the effect of changing individual parameters on the NOE distance bound violations of the β -peptide. The following solute parameters were separately varied: backbone partial charges, force constants of backbone torsional-angle energy terms (changes up to ± 20 %), and C12 repulsive van der Waals parameters of GROMOS atom types (Oostenbrink et al. 2004) C, O, N, CH1, CH2, and CH3 (changes up to ± 10 %). The results for changes from the 53A6 force field are shown in Fig. 3. The biggest effect comes from the change in backbone atomic partial charges. Increasing them improves the agreement with the experimental NOE



Fig. 4 Sum of the positive NOE distance bound violations for the α -peptide predicted by one-step perturbation using the $P\alpha_{-}53A6$ simulation as the reference state and varying different force-field parameters

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data, and vice versa. This may be due to stabilization of the helical conformation of the β -peptide over the nonhelical ones by the increase of backbone partial charges. Increasing or decreasing the force constants of backbone torsionalangle energy terms has only a very small effect on improving or impairing the agreement with the experimental data. Decreasing the repulsive C12 van der Waals parameters improves the agreement except for the atom type CH3.

For the hepta- α -peptide, similar conclusions were obtained for the changes in backbone torsional-angle force constants and C12 parameters of the backbone atoms (Fig. 4). However, an opposite relation between force-field parameters and NOE violations was observed for the change of backbone partial charges; i.e., reducing the backbone partial charges improves the agreement with the experimental NOE data for the α -peptide. This may be caused by the α -peptide adopting predominantly unfolded conformations (Wang et al. 2010). Increasing the backbone partial charges destabilizes unfolded conformations over helical ones, and thus impairs the agreement with experimental data for the α -peptide while it improves the agreement for the β -peptide. This observation nicely demonstrates that force-field parameters should not be obtained based on single simulations of macromolecules. A quantity $O(\vec{r}^N)$ may pose conflicting requirements on force-field parameters for different systems, and different quantities $Q(\vec{r}^N)$ may show conflicting requirements for a single system. This illustrates the challenge of transferable force-field development.

In summary, one-step perturbation, which in this case is equivalent to reweighting configurations, constitutes an efficient technique to predict violations of NOE distance bounds of peptides upon changing force-field parameters. However, a necessary condition is that conformations relevant to both Hamiltonians be present in the conformational ensemble used to obtain $\langle Q \rangle$ values. Reweighting can also be used to predict quantities $\langle Q \rangle$ other than NOE distance bound violations such as X-ray diffraction intensities, residential dipolar couplings, or circular dichroism (CD) spectra for a particular system, which makes it a powerful technique for force-field development that easily reduces the number of required separate simulations by an order of magnitude.

Acknowledgments This work was financially supported by the National Center of Competence in Research (NCCR) in Structural Biology and by grant number 200020–137827 of the Swiss National Science Foundation, and by grant number 228076 of the European Research Council (ERC), which is gratefully acknowledged.

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