Revealing Plastic Deformation Mechanisms in Polycrystalline Thin Films with Synchrotron XRD

Ralph D. Nyilas, Stephan Frank, and Ralph Spolenak

Understanding the fundamentals of plastic deformation mechanisms in polycrystalline thin metal films and the associated size effects is crucial to the design and fabrication of microelectronic devices. A combination of in-situ synchrotron diffraction experiments was conducted to investigate two cooperative plastic deformation mechanisms in polycrystalline face-centered cubic thin metal films: conjugate deformation twinning in uniaxially strained polycrystalline thin gold fi lm and subgrain structure rotations in biaxially strained polycrystalline thin silver films. The experimental results demonstrate an increase in the total coverage of (115) oriented deformation twins in the thin gold films upon uniaxial deformation to 2% strain at a macroscopic yield stress of 250 MPa.

INTRODUCTION

With the continuing miniaturization of microelectronic devices, a fundamental understanding of size effects associated with the mechanical response of polycrystalline thin film materials on the mesoscopic scale (1-10 micrometers) is crucial to ensure mechanical and electronic reliability by the control of microstructure.1 The dimensional and microstructural constraints in operating microelectronic devices such as, for example, conductor lines in integrated circuits, thin film materials in CMOS transistors, or thin metals films on polymer substrates are known to lead to high intrinsic stresses inducing failure by such mechanisms as passivation cracking,¹ hillock formation,^{2,3} electromigration,4,5 or cracking.6,7

While plastic deformation of face centered cubic (f.c.c.) metals during the early stages occurs primarily by dislocation glide on the most highly stressed

How would you... ...describe the overall significance of this paper?

In this work, the plastic deformation mechanisms of uniaxially and biaxially strained polycrystalline thin films are investigated using a combination of in-situ synchrotron diffraction techniques. From the measured geometry of the deformation patterns in the uniaxially strained films a conjugate twinning mode of plastic deformation is suggested. For the biaxially strained films, subgrain structure rotations are demonstrated and the plastic deformation mechanism understood by employing a disclination model. ... describe this work to a materials science and engineering professional with no experience in your technical specialty? In this paper, two distinct plastic deformation mechanisms are investigated in polycrystalline thin films using in-situ synchrotron diffraction. The experiments demonstrate a conjugate deformation twinning mode in uniaxially strained thin gold films and subgrain structure rotations in biaxially strained films. The in-situ synchrotron diffraction experiments

allow tracking the evolution of local misorientations and straining fields upon deformation.

a ...describe this work to a layperson?

The mechanical properties of materials change drastically when a characteristic length, such as a film thickness, reaches the micrometer scale. An example is the increase in yield strength with decreasing film thickness. In this work, a combination of advanced x-ray techniques is used allowing the non-destructive measurement of the evolution of crystallographic orientations and strains upon deformation of thin film specimens on the micrometer scale.

{111}<110> slip system, the dislocation density on secondary slip systems is known to increase continuously upon deformation, leading to another mode of plastic deformation involving the cooperative movement and arrangement of partial dislocations: deformation twinning. In particular, with the onset of stage III hardening^{8,9} in low stacking fault energy f.c.c. metals at room temperature, relatively high activation energy and high stresses are required for deformation by primary dislocation cross-slip. It has been demonstrated that size effects in thin metal films favor deformation by partial dislocation motion over perfect dislocation glide with decreasing film thickness.10-12 For conjugate deformation twinning, the transformation of Burgers vectors and lattice planes between parent and twin lattices are determined by symmetry operations of the crystal lattice as specified by the correspondence matrix.13

A different cooperative mode of plastic deformation involves subgrain structure rotations due to changes in the total Burgers vector content of dislocated boundaries such as geometrically necessary dislocation boundaries (GNBs). In contrast to deformation twinning, the structure rotation is in this case not constrained to be a symmetry operation of the crystal lattice. In the present work, a combination of synchrotron x-ray diffraction techniques is employed to investigate the fundamentals of these two plastic deformation mechanisms on the mesoscopic scale in polycrystalline thin f.c.c. films.

Transmission electron microscopy (TEM) studies have shown that the evolution of misorientation angles of geometrically necessary dislocation boundaries (GNBs) and incidental dislocation boundaries (IDBs) are directly correlated with the macroscopic applied strain deformation^{14,15} and revealed a scaling behavior in both the spacing between GNBs and the cor-

responding misorientation angles with accumulated plastic strain.^{16,17} To include cooperative dislocation effects in a mesoscale plasticity model, i.e. the effect of the collective evolution of dislocation substructures and lattice incompatibilities on multiple length scales, the importance of the concept

EXPERIMENTS AND METHODS

In Situ Synchrotron X-ray Diffraction

Uniaxially Strained Polycrystalline Gold Films

Polycrystalline thin gold films were prepared by direct current magnetron sputter deposition (PVD products) on Kapton® HN substrate sheets (DuPont, thickness of 125 µm) under high vacuum conditions (10⁻⁷ mbar) at a sputtering power of 360 W corresponding to a total deposition rate of about 1 nm s⁻¹. The Ar⁺ pressure was maintained at 40.10⁻³ mbar during deposition. The film thickness was measured by focused ion beam (FIB) preparation showing a homogenous film thickness of 1.8 µm. After deposition, the samples were annealed in a separate vacuum annealing oven at 450°C for 3 hours achieving an average grain size of several micrometers. Square shaped fiducial markers were prepared by FIB milling to allow correction of the reference coordinates during the in-situ microdiffraction experiment. Two sets of in-situ synchrotron experiments were conducted on the prepared samples, the first conducted at the MS beamline (X04SA) for the determination of the macroscopic principle film stresses during uniaxial straining, the second at the microdiffraction beamline (X05LA), both at the Swiss Light Source (SLS).

The synchrotron based method for the in-situ measurement of principle film strain components originates from the work of Böhm et al.³⁴ and has been transferred to the MS beamline (X04SA) at the SLS³⁵ as described in references 7 and 36. The energy of the incident synchrotron x-ray beam was tuned to 7.97 keV. The (111) fiber texture of the films required a beam energy of 7.97 keV in order to fulfill the diffraction conditions for the (111) planes which are at an angle of 70.53° with respect to the sample surface. Two second generation microstrip detectors^{37,38} have been mounted in the load direction and transverse to the load direction to measure changes in lattice plane distances. The reference spectrum for calibration of the detector modules was obtained from a tungsten powder, dispersed in vacuum grease, which was applied to the backside of the Kapton substrate. The sample was strained in-situ up to approximately 5%



Figure A. (a) Experimental setup of the in-situ synchrotron tensile experiment at the MicroXAS beamline (X05LA) of the SLS. The synchrotron x-ray beam is focused to a micrometer spot size by the KB mirror optics (3) and intercepts the gold sample parallel to the film surface normal in a transmission geometry ($2\theta=0^{\circ}$). The arrows indicate the diffraction cone and the experimental components are numbered as (1) Photonic Science CCD, (2) tensile stage, (4) translation stage, (5) beam stopper. The inset shows a transmission diffraction pattern. (b) Experimental setup at the microdiffraction beamline of the ALS (beamline 12.3.2). In the experiment biaxial strains are thermally imposed on the sample (polycrystalline thin silver films). The figure shows the sample stage (2) in a back-diffraction geometry ($2\theta=90^{\circ}$). The sample stage consists of a resistive heating element and a glass ceramic unit with an extremely low thermal expansion coefficient (10^{-7} K⁻¹).

strain comprising a total of 65 loading and 45 unloading steps using a mounted tensile stage (Kammrath and Weiss). After each strain step an automatic readout procedure of the microstrip detectors was performed to record the diffracted intensities in loading and transverse directions.

In the microdiffraction experiment conducted, gold samples of the same batch have been strained in-situ using the same tensile stage in transmission diffraction geometry at the microdiffraction beamline X05LA at the SLS. The experimental setup and geometry together with a representative Laue diffraction pattern is shown in Figure Aa. The synchrotron x-ray source emerges from an undulator insertion device in the energy range between 5–18 keV. The pre-optics and KB mirrors were optimized to achieve a focused beam spot size of $1.0 \times 1.4 \,\mu$ m (vertical × horizontal). A separate calibration sample of a (100) oriented single crystal silicon (thickness of 50 μ m) has been used for calibration. The sample was strained up to a total strain of 2% comprising seven strain steps. After each strain step Laue diffraction frames over a sample area of 40×40 μ m were collected corresponding to a lateral step size of 1 μ m using a photonic science CCD area detector (Figure Aa).

Biaxially Strained Polycrystalline Silver Films

Polycrystalline thin Ag films (1 μ m film thickness) were prepared by direct current magnetron sputter deposition (PVD products) on (100) oriented silicon substrates (thickness of 150 μ m coated with a 50 nm amorphous diffusion barrier). Sputter deposition was carried out under high vacuum conditions (~10⁻⁷ mbar) at a sputtering power of 200 W and Ar⁺ pressure of 40·10⁻³ mbar yielding a total sputter rate of 1.7 nm s⁻¹. After deposition the samples were annealed in the sputter chamber for two temperature cycles starting from room temperature to 450°C. The biaxial stresses were measured during two hysteresis cycles by the wafer curvature method¹ by the deflection of a two-dimensional (2-D) array of parallel laser spots (kSA multibeam optical sensor technology). At room temperature the biaxial film stresses are tensile (70 MPa). Compressive stresses develop in

the film as the temperature is increased up to about 150°C when the film starts to yield macroscopically.

The microdiffraction experiment was conducted at the microdiffraction beamline (12.3.2) at the Advanced Light Source (ALS). The beamline provides micrometer focused x-rays (vertical and horizontal FWHM of 1 μ m) from a superconducting bending magnet in the energy range between 5–20 keV.^{27,28} The experimental setup and back-diffraction geometry together with a microdiffraction pattern is shown in Figure Ab. The sample was strained in-situ by heating the sample in four intervals up to a temperature of about 150°C. To locate the fiducial platinum markers on the sample, 2-D fluorescence scans were taken over the area of interest at each temperature. The sample was translated relative to the incoming x-ray beam with a lateral step size of 0.5 µm to scan over the polycrystalline ensemble of interest $(20 \times 20 \ \mu m^2)$ corresponding to a total of 1,600 Laue diffraction frames per temperature. The silicon reference peaks from the substrate (Figure Ab) were used for detector calibration.

of disclinations has been generally acknowledged.18,19 It has been demonstrated that partial disclination multipoles may be formed during polycrystalline deformation due to incompatibilities in both, plastic strain and rotations of adjoining crystalline domains.²⁰⁻²² At the same time, disclination models of deformation twinning have been shown to be important in understanding the mechanism of the generation of secondary twins.²³⁻²⁶ To date, fundamental open questions remain concerning the two plastic deformation modes in thin metal films. Concerning the twinning deformation mode in low stacking fault energy f.c.c. thin metal films, the question is raised how the dislocation substructure inherited from the parent transforms to the deformation twin generated and the strains necessary to increase the fraction of grains in a twin orientation. Concerning the second plastic deformation mode by subgrain structure rotations, the objective is to understand the rotational deformation mechanism employ-



Figure 1. (a) Principle stress components in loading (σ_x) and transverse (σ_y) directions of the thin gold film as a function of total strain determined from the relative principle lattice strains from the in-situ synchrotron tensile experiment conducted at beamline X04SA at the SLS. At a strain of 0.006 the macroscopic yield stress of 250 MPa is reached and the sample starts to work harden. (b) Evolution of the (111) peak width with applied uniaxial strain.

ing a mesoscale model of plasticity.

The importance of the synchrotron xray microdiffraction technique to study mesoscale distributions of crystallographic orientations, lattice strain, and plastic deformation patterns has been amply demonstrated.²⁷⁻³³ In this work, in-situ synchrotron diffraction experiments have been conducted at the MS beamline (X04SA) and microdiffraction beamline (X05LA) at the Swiss Light Source (SLS) as well as at the microdiffraction beamline 12.3.2 at the Advanced Light Source in Berkeley, California. The synchrotron experiments at the Swiss Light Source comprised in-situ uniaxial tensile experiments on thin gold films in transmission geometry. The microdiffraction experiments at the Advanced Light Source (ALS) were conducted in back-diffraction geometry while biaxial strains have been imposed by temperature cycling.

See the sidebar for a description of the experiments and methods.

RESULTS

Conjugate Deformation Twinning in Polycrystalline Thin Gold Films

The relative principle lattice strains were determined from the measured

change in lattice spacing in transverse and loading directions following the method of Böhm et al.34 The principle stress components in loading and transverse directions of the thin gold film is plotted versus the total strain in Figure 1a. The macroscopic yield stress of the gold film of 250 MPa is reached at a strain of 0.6% as seen in Figure 1a. After an initial small load drop, the gold film starts to work harden. Note that only relative stresses and not residual stresses are determined from the relative lattice strains. Residual stresses can also be in principle determined from the difference in the stress plateaus between loading and unloading cycles which in the present case is not significant as seen in Figure 1a.

The Laue microdiffraction patterns (1,600 diffraction frames for each strain step) collected during the in-situ microdiffraction tensile experiment (Figure Aa) have been indexed using the XMAS code.²⁷ Complete pole figures have been constructed for each strain step from the indexed Laue microdiffraction patterns corresponding to an area of $40 \times 40 \ \mu m$ over the polycrystalline ensemble.

Figure 2 shows complete {111}, {100}, and {115} pole figures for two different strains, i.e. 0.6% and 2%. The



Figure 2. Pole figures constructed from 1,600 indexed Laue microdiffraction patterns corresponding to the total scanned area over the polycrystalline ensemble of 40×40 μm. The {100} pole figure shows the random in-plane orientation of the {100} planes corresponding to the {100} ring in the pole figure. A fraction of the grains is 115 out of plane oriented as seen by the central peak in the {115} pole figure. (c) The total coverage of (111) and (115) out of plane oriented grains up to 2% strain. The color code in the contours scales with the density of points.

{111} pole figures show the (111) out of plane texture of the gold film while the {100} pole figures show a corresponding random in-plane orientation. The majority of grains are (111) out of plane oriented while the remaining fraction is (115) out of plane oriented as seen by the central peak in the {115} pole figures. The total grain coverage of the (111) out of plane and (115) out of plane oriented grains was determined from the complete pole figures for each strain step. Figure 2c shows the total coverage of (111) and (115) out of plane oriented grains up to 2% strain. The decrease in the grain coverage of the (111) oriented grains is accompanied by an increase in the grain coverage of the (115) oriented grains. The increase in the fraction of the secondary texture component up to 2% strain is also consistent with the texturing effect observed on the macroscopic scale using a monochromatic synchrotron x-ray beam during the in-situ tensile experiment on the same batch of samples at the MS beamline (X04SA). Figure 1b shows the continuous increase in peak width of the (111) peak which accompanies the continuous decrease in the total area under the (111) diffraction peak between 0.6 and 2% strain (decrease by approximately 40%) as determined by numerically integrating the diffracted intensity of the (111) peak with respect to 2θ .

Figure 3 shows contour plots of the smallest angle between the surface normal and the <115> directions over a selected area of the polycrystalline ensemble for two different strain states. The grains have been identified by constructing pole figures over the selected grain areas (Figure 3). The figure shows the {111} pole figures of the (111) oriented grains (grains numbered from 1 to 4) corresponding to the two different strain states. The (115) oriented grains have been identified in the same way and numbered in Figure 3 demonstrating that a new (115) oriented deformation twin has developed between two of the (111) oriented grains (between grains 1 and 4).

Subgrain Structure Rotations in Polycrystalline Thin Silver Films

The Laue microdiffraction patterns were indexed using the XMAS software package^{27,28} which allows indexing



Figure 3. Contour plots of the smallest angle between the surface film normal and the <115> crystallographic direction over a selected area of the polycrystalline ensemble for two different strain states. The pole figures below show the crystallographic orientations of the four (111)-oriented grains numbered from 1 to 4 in the contour plots for the two different strain states. At 0.06% strain the contour plot shows a new (115) deformation twin between the (111)-oriented grains (between grain 1 and grain 4). The transformation of Burgers vectors and lattice planes between deformation twin and matrix is discussed in the text.







overlapping Laue patterns originating from differently oriented grains. The crystallographic orientations have been determined from the absolute peak positions, while the relative peak shift of the indexed peak positions allowed to determine the deviatoric strain tensor components with strain sensitivity of about $2 \cdot 10^{-4}$.

0.13°).

Following the evolution of both crystallographic orientations and the deviatoric stress state from room temperature to 150°C, we observe stress driven grain rotations and subgrain dislocation structure formations leading to plastic deformation heterogeneities. Figure 4 shows contour maps of both, the in-plane crystallographic orientation and the deviatoric stress tensor components over the polycrystalline ensemble of interest for different applied biaxial strain states (i.e., sample temperatures). Within the central grain (numbered as grain 1 in Figure 4) dislocated walls have formed as determined by scanning the indexed Laue peaks across and along the misoriented crystalline domains. Scanning the indexed Laue peaks across the dislocated walls, the indexed peaks split into two discontinuous intensity maxima, while the peaks split into characteristic three peaks at triple lines where three misoriented crystalline domains meet.

As the temperature increases from 60°C to 85°C the crystal volume of the grain of interest (numbered as 1) rotates relative to the fixed sample reference

frame (as verified by tracking the orientation of silicon reference pattern) as shown by the evolution of the in-plane orientation along a profile through the grain (Figure 5). As the temperature increases to 85° the grain is subject to a shear stress gradient (corresponding to a shear stress difference of 100 MPa) and a stress gradient in the normal stress component as shown in Figure 4. Upon a further increase in applied biaxial strain to 115°C a subgrain structure forms within the grain as shown in the in-plane orientation contour in Figure 4. The in-plane misorientation between the corresponding crystalline domains of the subgrain is about 1.4° (Figure 5). The shear stress gradient within the grain relaxes upon the substructure formation as seen in Figure 4.

DISCUSSION

Conjugate Deformation Twinning in Polycrystalline Thin Au Films

In this section the mechanism of the observed generation of deformation twins upon uniaxial strain deformation is discussed by analyzing the transformations of the dislocation substructure from parent to twin for conjugate twinning. The theoretically expected transformations of the primary dislocations are determined and compared to the experimental results by analyzing the streak patterns in the Laue microdiffraction patterns. A specific dislocation mechanism, based on the pole mechanism, is discussed to describe the cooperative movement of the twinning dislocations generating the mesoscale deformation twins.

The crystallography of twinning is described by four independent twinning elements, two invariant undistorted planes (twinning plane and conjugate twinning plane) and two directions (direction of the twinning shear strain and conjugate twinning direction).13,39 The twinning elements are identified by shearing a Thompson tetrahedron on successive (111) planes above the twinning plane by a partial Burgers vector (a/6 < 112)). The conjugate twinning plane rotates to a different plane in the twin, while the twinning plane remains unchanged. For twinning of type I according to the classification of Bilby et al.,39 the transformation between the crystallographic lattices and planes between parent and twin is accomplished by a homogeneous shear deformation gradient. The reindexation matrix U specifies the transformation (rotation of π about the normal to the twin plane) between the crystallographic vectors in the parent to the ones in the twin orientation, while the correspondence matrix C describes the transformation of Burgers vectors from the parent to



Figure 6. (a–c) Schematic illustrating the transformation of the primary mobile $a/2[101]^T$ dislocation and the twinning Shockley dislocation $a/6[121]^T$ to the sessile $a/6[424]^T$ dislocation (with reference to the matrix or parent coordinate system). When reindexed using the reindexation matrix U, the sessile $a/6[424]^T$ dislocation corresponds to the $a/2[0-20]^T$ dislocation with respect to the twin coordinate system. (d) Laue streak simulation to the microdiffraction patterns of (111) oriented parent, and (e) (115) oriented deformation twin.

the twinned lattice including the shear deformation.13,40 (See Equations 1 and 2; all equations are shown in the table.) Using the reindexation matrix U, the crystallographic orientation of the conjugate twins corresponding to a (111) orientation of the parent lattice is the (115) orientation in the twinned lattice, consistent with the secondary (115) texture in Figure 2 (see Equation 3). (In the notation used, column vectors are denoted as the transpose of row vectors using the superscipt T. The Einstein summation convention of a repeated index being summed is used throughout the paper.)

In Figure 6a–c, the transformation of a primary dislocation a/2 $[101]^{T}$ with the partial twinning dislocation a/6 $[121]^{T}$ to a sessile a/6 $[\overline{424}]^{T}$ dislocation is illustrated in the reference frame of the parent crystal. The sessile a/6 $[\overline{424}]^{T}$ dislocation corresponds to the a/2 $[0\overline{10}]^{T}$ sessile dislocation (on the (100) plane) when reindexed (using the reindexation matrix **U**) to the twin reference frame. Using the correspondence matrix **C**, the primary

Equations						
$U = \frac{1}{3} \begin{pmatrix} 1 & -2 & 2 \\ -2 & -1 & -2 \\ 2 & -2 & -1 \end{pmatrix}$	(1)					
$C = \frac{1}{2} \begin{pmatrix} -1 & -1 & 1 \\ -2 & 0 & -2 \\ 1 & -1 & -1 \end{pmatrix}$	(2)					
$U(111)^{T} \to (\overline{15}\overline{1})^{T}$	(3)					
$\frac{a}{2}[101]^{T} + \frac{a}{6}[121]^{T} = \frac{a}{6}[424]^{T}$	(4)					
$U\left(\frac{a}{6}[424]^{T}\right) = a[0\overline{1}0]^{T}$	(5)					
$\boldsymbol{b}_t = \boldsymbol{C} \boldsymbol{b}_m$	(6)					
$\Omega_{j} = \oint_{c} \kappa_{ij} dx_{i}$	(7)					
$\mathbf{Y}_i = \mathbf{A}_{ij}\mathbf{X}_j$	(8)					
$A = \begin{pmatrix} \cos(\theta_A) & -\sin(\theta_A) & 0\\ \sin(\theta_A) & \cos(\theta_A) & 0\\ 0 & 0 & 1 \end{pmatrix}$	(9)					

Table I. Misorientation Angles Corresponding to the Transformation Paths in Figure 7a								
Transformations	Α	В	С	D	К	Н	DCBA	
60°C Rotation angle (°)	+1.14	-0.78	+0.98	-0.60	+1.09	-1.10	0.74	
85°C Rotation angle (°)	0.69	-0.36	+1.25	-0.68	+1.00	-0.95	0.90	

mobile $a/2 [101]^T$ dislocation is directly transformed to the sessile $a/2 [0\overline{1}0]^T$ dislocation in the twin reference frame according to the transformation shown in Equations 4 and 5.

Note that the transformations leading to the generation of the conjugate twin extend over two nodes as illustrated in Figure 6b. To investigate the twinning mechanism, the transformation of Burgers vectors between deformation twin and parent lattice is examined from the streaking of the indexed peaks in the Laue microdiffraction patterns between the (115) oriented deformation twins and the (111) oriented parent lattice in Figure 3. The streaking of the Laue microdiffraction peaks has been simulated by introducing geometrically necessary dislocations (GNDs) on the primary <110>(111)slip system and tracking the corresponding cooperative movement of the Laue peaks for each of the 12 possible slip systems using the XMAS software package.^{27,28} The simulated Laue streak pattern is superimposed on the Laue diffraction patterns in Figure 6d corresponding to the (111) oriented grain (grain 1) in Figure 3. The slip system representing the best fit between simulated and measured streaks is

obtained for the Burgers vector $\mathbf{b}_{m} =$ $[\overline{1}0\overline{1}]^{T}$ and slip plane normal $\mathbf{n}_{m} =$ $[\overline{1}\overline{1}1]^{T}$. The Laue microdiffraction pattern of the (115) oriented deformation twin (grain 7) is shown in Figure 6e. Laue streak simulations have been performed for the <111>(110), the <110>(001) as well as the <010>(100)system. The best fit to the experimental Laue streak pattern was obtained for the Burgers vector $\mathbf{b} = [0\overline{1}0]^{T}$ and plane normal $\mathbf{n} = [\overline{1}00]^{T}$ and is shown in Figure 6e. The transformations of Burgers vectors and lattice planes as demonstrated in the experimental Laue patterns is consistent with the transformation for conjugate deformation twinning as specified by the correspondence matrix C (see Equation 6).

The pole mechanism, first proposed by Cottrell and Bilby,⁴¹ provides an elegant dislocation mechanism for the growth of the conjugate twin starting with one layer of a stacking fault. The primary a/2 [101]^T dislocation (compare to Figure 6a) is first dissociated into two Shockley partials thereby distorting the twinning plane in a helical topology. The intersecting twinning dislocations (a/6 [121]^T) wind around the dissociated primary dislocation (pole dislocation) generating a mono-



Figure 7. Representation of the system of closed dislocated walls in terms of partial wedge disclination multipoles (b). Transformation paths (in red) around the disclination multipoles (a). The arrows indicate the directional sense of the transformations of a vector as the dislocation wall is crossed and the bold letters the corresponding transformation matrices. The product of transformations corresponding to a transformation path around the branching dislocation walls (DCBA) is equal to the rotational closure failure corresponding to a Burgers circuit around contour C

layer of stacking fault after each spiral turn. In the present case, the thin film geometry is expected to enhance the driving force for such mechanisms as (i) dissociation of perfect dislocations is in general favored due to the size effect in thin film geometries, (ii) cross-slip and climb force components are enhanced due to image forces, (iii) pinning points for the pole dislocation may be provided at the substrate-film interface and the free surface of the film.

Subgrain Structure Rotations as a Manifestation of Changes in Burgers Vector Content

To understand the mesoscale rotational deformation of the grain, the plastic deformation heterogeneities comprising the system of branching dislocation walls (Figure 4) are idealized by partial wedge disclination dipoles (Figure 7). Figure 7a illustrates the transformation paths across the branching dislocated walls of the system of dislocation boundaries. The misorientation angles for the corresponding transformation paths are summarized in Table I.

In analogy to the Burgers vector specifying the translational closure failure of a Burgers circuit around a dislocation line, the Frank vector specifies the rotational closure failure of a Burgers circuit around a disclination line leading to rotational displacements of adjacent volumes of material. Any disclination may be represented by a superposition of dislocations, the simplest example is the wedge disclination dipole (in which the Frank vector is parallel to the disclination line). For review on current state of the art and theory of disclinations reference is made to the work of Romanov and coworkers.18,19

Consider a Burgers circuit around the multipole disclination configuration as illustrated by the contour path C in Figure 7. The rotational closure failure Ω for this contour path is specified by the closed loop integral of the local curvature tensor, as shown in Equation 7, where κ is the curvature tensor⁴² relating infinitesimal changes in lattice rotations about an orthonormal vector basis (dx_i) to the corresponding displacement field. For wedge disclination dipoles, the Frank vector is in the boundary plane and parallel to the disclination lines such that the curvature tensor has only two non-vanishing components, i.e. $\kappa_{13} \neq 0$ and $\kappa_{23} \neq 0$. For this case Equation 7 can be expressed in terms of the sum of the Frank vector strengths of the disclinations comprising the polygon of closed dislocation walls. The transformation matrix A specifies the transformation of a vector x, to y, as one of the dislocation walls is crossed, (Eqution 8), where the transformation matrix is specified by the corresponding misorientation angle θ_{Λ} as Equation 9.

The rotational closure failure in Equation 7 is determined by the product of the transformation matrices corresponding to a transformation path around the multipole disclination configuration (DCBA) in Figure 7a. The rotational closure failure corresponding to this closed path as determined from the measured misorientation angles is summarized in Table I. The rotational closure failure increases from 60° C to 85° C by 0.90° - $0.74^{\circ} = 0.16^{\circ}$. The rotation angle compares well with the in-plane rotation of the grain between 60°C and 85°C (Figure 5). This result suggests that the rotational deformation of the grain is a manifestation of the change in the rotational incompatibilities comprising the coupled system of multifold branching dislocation walls. Note the analogy to the case of a translational closure failure in which the circulation (contour integral) of the displacement gradient tensor determines the total Burgers vector. The analogous field quantities are the displacement gradient tensor and curvature tensor field ĸ, Nye's dislocation density tensor and the disclination density, the total Frank vector Ω and the total Burgers vector. Any change in the local source terms (any Frank vector of the partial disclinations) determines the mechanical response of the coupled system (in the present case the structure rotation) comprising the system of dislocated walls. The observed mesoscale rotational deformation of the grain is directly related to structural transformations of the dislocation substructure heterogeneity. Synchrotron experiments conducted at the SLS on polycrystalline thin gold films revealed stress driven rotational plastic deformation mechanisms similar to the ones reported here.22 It is important to note that in both studies, the thin films investigated comprised low stacking fault energy metals of different stacking fault energies, i.e. gold (55 mJm⁻²)43 and silver (17 mJm⁻²)⁴³ films. A partial disclination dipole may be represented as a mesoscopic partial dislocation with an effective Burgers vector dependent on the length of the dipole arm and the Frank vector strength. Analogous to the partial dislocation bordering a stacking fault for which the partial Burgers vector is not a translational symmetry operation, the Frank vector of a partial disclination is not a rotational symmetry operation.

CONCLUSIONS

In-situ synchrotron diffraction experiments on polycrystalline thin gold films reveal the generation of conjugate deformation twins upon uniaxial deformation. Film stresses in the loading and perpendicular direction have been determined from the measured relative lattice strains yielding a macroscopic yield stress of about 250 MPa. The microdiffraction experiments demonstrate that the total coverage of grains in the secondary (115) twin orientation increases upon uniaxial strain deformation at the expense of the total coverage of the (111) oriented grains. By analyzing the streak patterns in the Laue microdiffraction frames between parent and deformation twin, the transformation of Burgers vectors and lattice planes is demonstrated and shown to be consistent with the correspondence matrix for conjugate deformation twinning. The second plastic deformation mechanism investigated, comprised subgrain structure rotations upon biaxial deformation in polycrystalline thin silver films. In the in-situ microdiffraction experiments the sample was subjected to biaxial strains. The evolution of local strains and crystallographic orientations demonstrated a stress driven subgrain rotation leading eventually to a new subgrain structure. The observed rotational mechanical response is understood as the change in total Burgers vector content comprising the system of dislocated boundaries.

ACKNOWLEDGEMENT

The kind support and discussions with beamline scientists Nobumichi Tamura and Martin Kunz from the Advanced Light Source are acknowledged. Also special thanks to Daniel Grolimund for his support during our beamtimes at the Swiss Light Source.

References

1. W.D. Nix, *Materials Transactions*, 20A (1989), pp. 2217–2245.

- 2. D.-K. Kim et al., *Thin Solid Films*, 371 (2000), pp. 278–282.
- 3. F.Y. Genin and W.J. Siekhaus, J. Appl. Phys., 79 (1996), pp. 3560–3566.
- 4. B.C. Valek et al., *J. Appl. Phys.*, 94 (2003), pp. 3757– 3761.
- 5. B.C. Valek et al., *Appl. Phys. Lett.*, 81 (2002), pp. 4168-4170.

6. T. Li and Z. Suo, Int'l. J. Solids and Structures, 43 (2006), pp. 2351–2363.

7. S. Frank et al., Acta Materialia, 57 (2009), pp. 1442– 1453.

8. A. Seeger, *Work Hardening* (New York: Gordon & Breach, 1968).

9. A. Seeger et al., *Philosophical Magazine*, 2 (1957), pp. 323–350.

10. S.H. Oh et al., *Acta Materialia,* 55 (2007), pp. 5558– 5571.

11. G. Dehm et al., Acta Materialia, 55 (2007), pp. 6659-6665.

12. M. Chen et al., Science, 300 (2003), pp. 1275-1277.

Ralph Spolenak is a TMS Member!

To read more about him, turn to page 9. To join TMS, visit www.tms.org/Society/Membership.aspx.

13. J.W. Christian and S. Mahajan, *Progress in Materials Science*, 39 (1995), pp. 1–157.

14. D.A. Hughes et al., *Scripta Materialia*, 48 (2003), pp. 147–153.

15. D.A. Hughes et al., *Acta Materialia*, 45 (1997), pp. 105–112.

16. A. Godfrey and D.A. Hughes, *Acta Materialia*, 48 (2000), pp. 1897–1905.

17. A. Godfrey and D.A. Hughes, *Scripta Materialia*, 51 (2004), pp. 831–836.

18. A.E. Romanov and V.I. Vladimirov, *Dislocations in Solids* (Amsterdam: North Holland, 1992).

19. A.E. Romanov, *European J. Mechanics - A/Solids*, 22 (2003), pp. 727–741.

20. V.V. Rybin et al., *Acta Metallurgica et Materialia*, 41 (1993), pp. 2211–2217.

21. A.A. Zisman and V.V. Rybin, *Acta Materialia*, 44 (1996), pp. 403–407.

22. R.D. Nyilas et al., *Acta Materialia*, 57 (2009), pp. 3738–3753.

23. P. Müllner, *Solid State Phenomena*, 87 (2002), pp. 227–238.

24. P. Müllner and A.E. Romanov, *Acta Materialia*, 48 (2000), pp. 2323–2337.

25. P. Müllner et al., *Acta Metallurgica et Materialia*, 42 (1994), pp. 1727–1732.

26. P. Müllner, *Scripta Metallurgica et Materialia*, 33 (1995), pp. 1181–1186.

27. N. Tamura et al., *J. Synchrotron Rad.*, 10 (2003), pp. 137–143.

28. N. Tamura et al., *Materials Science and Engineering: A*, 399 (2005), pp. 92–98.

29. R.I. Barabash et al., in: *Encyclopedia of Materials: Science and Technology* (Oxford, U.K.: Elsevier, 2001), p. 18.

30. R.I. Barabash et al., *Matls. Sci. and Eng. A*, 400-401 (2005), pp. 125–131.

31. R.I. Barabash et al., J. Appl. Phys., 93 (2003), pp.

5701-5706.

32. R.I. Barabash et al., *J. Appl. Phys.*, 93 (2003), pp. 1457–1464.

33. R.I. Barabash and P. Klimanek, J. Appl. Crystallography, 32 (1999), pp. 1050–1059.

34. J. Böhm et al., *Review of Scientific Instruments*, 75 (2004), pp. 1110–1119.

35. B.D. Patterson et al., Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, 540 (2005), pp. 42–67.

36. S. Olliges et al., Acta Materialia, 55 (2007), pp. 5201–5210.

37. B. Schmitt et al., *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment,* 501 (2003), pp. 267–272.

 B. Schmitt et al., Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, 518 (2004), pp. 436–439.

39. B.A. Bilby and A.G. Crocker, *Proc. Royal Society of London. Series A, Mathematical and Physical Sciences*, 288 (1965), pp. 240–255.

40. M. Niewczas, in: *Dislocations in Solids; Volume 13,* ed. F. Nabarro and J. Hirth (Dordrecht, The Netherlands: Elsevier, 2007), pp. 263–364.

41. A.H. Cottrell and B.A. Bilby, *Philosophical Maganzine*, 42 (1951), p. 573.

42. J.F. Nye, Acta Metallurgica, 1 (1953), pp. 153-162.

43. J.P. Hirth and J. Lothe, *Theory of Dislocations* (Columbus, OH: McGraw-Hill 1968).

Ralph D Nyilas, Stephan Frank, and Ralph Spolenak are with the Laboratory for Nanometallurgy, Department of Materials, ETH Zurich, Wolfgang-Pauli-Strasse 10, CH-8093 Zurich, Switzerland. Dr. Nyilas can be reached at ralph.nyilas@mat.ethz.ch.



hes, Acta Materialia, 48