Muon spin rotation and infrared spectroscopy study of magnetism and superconductivity in $Ba_{1-x}K_xFe_2As_2$

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(Received 25 October 2016; revised manuscript received 17 January 2017; published 22 February 2017)

Using muon spin rotation and infrared spectroscopy, we study the relation between magnetism and superconductivity in $Ba_{1-x}K_xFe_2As_2$ single crystals from the underdoped to the slightly overdoped regime. We find that the Fe magnetic moment is only moderately suppressed in most of the underdoped region where it decreases more slowly than the Néel temperature $T^N$. This applies for both the total Fe moment obtained from muon spin rotation and for the itinerant component that is deduced from the spectral weight of the spin-density-wave pair-breaking peak in the infrared response. In the moderately underdoped region, superconducting and static magnetic orders coexist on the nanoscale and compete for the same electronic states. The static magnetic moment disappears rather sharply near optimal doping, however, in the slightly overdoped region there is still an enhancement or slowing down of spin fluctuations in the superconducting state. Similar to the gap magnitude reported from specific-heat measurements, the superconducting condensate density is nearly constant in the optimally and slightly overdoped region, but exhibits a rather pronounced decrease on the underdoped side. Several of these observations are similar to the phenomenology in the electron-doped counterpart $Ba(Fe_{1−y}Co)y_2As_2$.

DOI: 10.1103/PhysRevB.95.054512

I. INTRODUCTION

Of great current interest is the relationship between magnetism and superconductivity (SC). The majority of unconventional superconductors are found proximate to a magnetic state which is reached by controlling some tuning parameter such as electronic doping, magnetic field, or pressure. It has also long been suspected that spin fluctuations are involved in the formation of the high-temperature SC state, perhaps also long been suspected that spin fluctuations are involved in the formation of the high-temperature SC state, perhaps in such materials [1–5]. The Fe-based superconductors (FeSCs) have highlighted that this proximity of magnetic and SC states can be taken one step further with magnetism and SC coexisting on a nanoscopic scale in these materials [6–10]. This is observed in lightly underdoped FeSCs where the two phases compete for the same electronic states. With further doping, a SC ground state without static magnetic order is obtained. The FeSCs are thus especially interesting systems for studying the changing relationship between SC and magnetism.

$BaFe_2As_2$ is a prototypical FeSC for such a study due to the high-quality, large single crystals that can now be synthesized. Its crystal structure is shown in Fig. 1(a), along with calculated muon-stopping sites (see details in Sec. III A), and an annotated phase diagram for the material is shown in Fig. 1(b). The key structural component is the FeAs layer as the (five) electronic bands crossing the Fermi level are predominantly of Fe-$3d$ character with a small admixture of As-$4p$ character [11]. The undoped parent compound is metallic and paramagnetic at high temperature with a tetragonal $I4/mmm$ space-group symmetry. Coincident with the Néel temperature $T^N$ of approximately 135 K is an orthorhombic distortion of the lattice and an antiferromagnetic (AF) state, annotated “o-AF” in Fig. 1(b). This AF state exhibits in-plane antiparallel spins along the $(0,\pi)$ direction and parallel ones along $(\pi,0)$ in a so-called single-$Q$ or striplike AF state [10]. The interactions underlying this magnetostructural transition are as yet unclear. Explanations range from itinerant models [12–14], in which Fermi-surface nesting governs the magnetic interactions, to local models which assume localized spins with exchange interactions determined by the orbital occupation [15,16]. It is probable that both itinerant and local models are partly applicable [10,17–19]. It has also been proposed that the spin-lattice coupling [20] and a near degeneracy of different spin states of the Fe ions [21,22] play an important role.

From this starting point, a combined SC and magnetic ground state can be induced. This can be by electrical doping with excess electrons by substitution of Ni or Co for Fe, with excess holes by substitution of Na or K for Ba, or by “chemical pressure” through the iso-valent substitution of P for As. Figure 1(b) shows the case for electron doping via Co substitution for Fe in $Ba(Fe_{1−y}Co)y_2As_2$ (BFCA), and for hole doping via K substitution for Ba in $Ba_{1−x}K_xFe_2As_2$ (BKFA). Infra-red (IR) optical spectroscopy [6,17], muon spin rotation ($\mu$SR) [6,8,9] and neutron scattering [23,24] have shown that the magnetic and SC states compete for the same electronic states in the underdoped region.

However, there are some signs of a qualitatively different relationship between magnetism and superconductivity in near optimally doped BFCA [open square symbols in Fig. 1(b)] [9]. In this regime, magnetic order or magnetic fluctuations...
In this work, we track the evolution of the magnetic and SC properties of BKFA in undoped ($x = 0$) to slightly overdoped samples ($x = 0.47$), shown by the open star symbols in Fig. 1, using $\mu$SR and infrared optical spectroscopy. $\mu$SR is a powerful technique for studying magnetism in the bulk. It is capable of measuring small magnetic fields, of order 0.1 mT, in true zero-external-field conditions. Since it is a probe of the local magnetic field at the muon site, rather than the volume-averaged magnetic field, it is possible to determine the volume fraction of a particular magnetic state. In turn, IR optical spectroscopy provides rich information about the bulk electronic properties. IR spectroscopy probes the energy, scattering, and symmetry of the SC gap(s) and sum rules can be used to determine the SC condensate density. The IR response of underdoped FeSCs also has a prominent spin-density-wave pair-breaking feature [34] that is related to the ordered magnetic moment from the itinerant carriers and is thus also a probe of the magnetic state. Combined, these two techniques provide a rich picture of the magnetic and SC states and the phenomenological relationship between them.

We find a coexistence and competition of static AF order and SC on a nanoscopic scale in single-crystalline BKFA for 0.19 \( \leq x \leq 0.26 \). The decrease in $T_N$ in this region is more rapid than the decrease in the local magnetic field, and the magnetic state is more ordered/uniform in BKFA than that of BFCA. We find an absence of static magnetic order in $x = 0.43$, but we do see an enhancement of spin fluctuations below $T_c$. In conjunction, the full SC volume fraction and in-plane London penetration depth $\lambda_L$ of approximately 200 nm at this doping level signals a robust SC state.

Our measurements complement previous optical studies on BKFA which have focused on the undoped [34,35] or optimally doped [36–41] compounds, with only a few studies of the underdoped compounds [17,42]. Similarly, previous $\mu$SR studies of BKFA have focused on near-optimally doped samples [26,27,43–45] with just one study of polycrystalline, underdoped samples [8]. On the other hand, BFCA has been more systematically studied by $\mu$SR [9,46] and IR optical spectroscopy [6,47].

The paper is laid out as follows. Experimental methods are discussed in Sec. II. We then present $\mu$SR results in Sec. III which show the development of the magnetic state.
in underdoped BKFA. The optical response is described in the following Sec. IV followed by a summary of results in Sec. V.

II. EXPERIMENT

High-quality single crystals of Ba$_{1-x}$K$_x$Fe$_2$As$_2$ (BKFA) were grown in alumina crucibles using an FeAs flux as described in Ref. [49]. The crystals were then characterized by x-ray diffraction refinement and electron dispersion spectroscopy. We did not detect impurity phases from these measurements. The K content, $x$, determined by these measurements indicates a small distribution of $x$ on the order of ±0.02. The estimated uncertainties in $x$ are indicated by the error bars in Fig. 1 and following figures. Resistivity and magnetization data were obtained with a Quantum Design PPMS.

The $\mu$SR measurements were performed at the GPS instrument of the $\mu$M3 beamline at the Paul Scherrer Institute (PSI) in Villigen, Switzerland. Fully spin-polarized, positive muons with an energy of 4.2 MeV were implanted in the crystal (along the c axis of the crystal) where they rapidly thermalize and stop at interstitial lattice sites distributed over a depth of about 100 $\mu$m. The muon spins precess in the magnetic field at the muon site $B_\mu$, with a precession frequency $\nu_\mu$, proportional to the magnitude of $B_\mu$, $B_\mu$, as $\nu_\mu = \gamma_\mu B_\mu / 2\pi$, where $\gamma_\mu = 2\pi \times 135.5$ MHz/T is the gyromagnetic ratio of the muon. The time evolution of the polarization of the muon spin ensemble $P(t)$ is detected via the asymmetry of the emission rate of the decay positrons as described in Refs. [50,51]. The zero-field (ZF) and transverse-field (TF) measurements were performed with the so-called up-down positron counters in spin-rotation mode for which the muon spin polarization $P_\mu$ is at about $54^\circ$ with respect to the muon beam (pointing toward the upward counter). See Fig. S7b of Ref. [18] for an illustration of the experimental geometry. The initial asymmetry in our experimental configuration is 0.21. Longitudinal-field (LF) measurements were performed with $P_\mu$ antiparallel to the muon momentum.

The far-infrared optical reflectivity $R(\omega)$ was measured from 45–700 cm$^{-1}$ with a Bruker Vertex 70v FTIR spectrometer with an in situ gold evaporation technique [52,53]. For the ellipsometry measurements we used a home-built rotating-analyzer setup attached to a Bruker 113v at 200–4500 cm$^{-1}$ [54] and for the near-infrared to near-UV region a Woollam VASE ellipsometer at 4000–52 000 cm$^{-1}$. We measured the in-plane component of the optical response representing an average of the a- and b-axis response [55,56] since the twinning of the samples was not controlled. The combined ellipsometry and reflectivity data have been analyzed as described in Refs. [53,57] to obtain the complex optical response functions; the complex optical conductivity $\sigma(\omega) = \sigma_1(\omega) + i\sigma_2(\omega)$ and the related complex dielectric function $\epsilon(\omega) = \epsilon_1(\omega) + i\epsilon_2(\omega) = 1 + 4\pi\sigma(\omega)/\omega$. The quantity $\int_{\omega_{\text{min}}}^{\omega_{\text{max}}} \sigma_1(\omega) d\omega$ is known as a spectral weight (SW) and is related by a sum rule [58] to the density of electronic states within the energy integration window $[\omega_{\text{min}}, \omega_{\text{max}}]$ by $\int_{\omega_{\text{min}}}^{\omega_{\text{max}}} \sigma_1(\omega) d\omega = \frac{2n_e e^2}{2m^*}$, where $e$ is the electron charge, $n$ is the density of electrons with energy within that window, and $m^*$ is the effective mass of those states. In the remainder of the paper we take the frequency dependence of these functions to be understood and drop the $(\omega)$ notation.

III. $\mu$SR

A. Zero-field $\mu$SR

In our study of the magnetic and SC response of BKFA we begin with the ZF-$\mu$SR data where the magnetic field at the
The clear oscillation frequencies for doped BKFA in Fig. 2 can be contrasted with BFCA where the magnetic signal is rapidly overdamped with Co substitution [9]. This is probably due to lower disorder in BKFA since the dopant ion is not on the FeAs layer. To be quantitative, we show in Fig. 3(a) a comparison of the low-temperature relaxation rates \( \lambda \) for BKFA and BFCA. While \( \lambda \) rapidly increases with Co doping from 3.3 \( \mu s \) for BFA to 50 \( \mu s \) for Ba(Fe_{0.96}Co_{0.04})_2As_2 where the first coexistence of SC and magnetism is seen, for BKFA \( \lambda \) remains a moderate \( \approx 10 \) \( \mu s \) well into the doping regime where SC is established. We note that the \( x = 0.23 \) sample has a slightly larger \( \lambda \), which may be due to a larger distribution of \( x \) values with respect to the other samples, or a larger degree of internal crystal strain. We also note that relaxation rates here
are smaller than those of Ref. [8], possibly because they were measuring polycrystalline rather than single-crystal samples.

We turn now to the low-temperature ZF-μSR oscillation frequency shown in Fig. 3(b). With increasing doping, \( T^N \) (dark-green squares) varies little between \( x = 0 \) and 0.19, but then falls rapidly at higher doping. Data from Böhmer et al. [28] (connected light-green squares) are overlaid which indicate \( T^N \) falls to zero at \( x = 0.3 \). In comparison, the low-temperature value of \( B_\mu \) (red circles) initially decreases even more slowly than \( T^N \). A similar observation was made in BFCA. Barring any change in the magnetic order and/or orientation of the magnetic moment, \( B_\mu \) is proportional to the magnetic moment on the Fe site. For \( x = 0 \), neutrons measure between 0.9 and 1 \( \mu_B/\text{Fe} \) [7] and with ZF-μSR we measure \( B_\mu = 0.210 \text{ T} (v_\mu = 28.4 \text{ MHz}) \), which is about 10% lower than expected from dipolar calculations based on a 0.9 \( \mu_B/\text{Fe} \) moment [18]. The relatively slow decrease of \( B_\mu \) strongly suggests that the magnetic moment on the Fe site decreases more slowly than \( T^N \) with doping. We can discount that a reorientation of the Fe moment contributes to these changes in \( B_\mu(x) \) since one can monitor the orientation of \( B_\mu \) by inspecting the signal from the orthogonal forward-backward detector set (see, for example, Fig. S7b of Ref. [18] for an illustration). Doing so shows that \( B_\mu \) remains parallel to the c axis (that means an in-plane Fe moment orientation), except in the t-AF phase of \( x = 0.26 \) between 32 and 18 K. We note that the gradual reduction in the Fe moment with doping in BKFA that we report here is in good quantitative agreement with very recent first-principles calculations [61]. The finding that \( T^N \) drops much faster than the low-temperature magnetic moment on the Fe site suggests that the two quantities are not directly related to each other. Indeed, experiments have shown that slowly fluctuating magnetic moments exist well above \( T^N \) [19]. The formation of a static long-range magnetic order at \( T^N \) may instead be tied to the near-concomitant tetragonal to orthorhombic structural transition discussed in the Introduction. Additional information can be gleaned from measuring the spectral weight of the spin-density-wave pair-breaking peak in the optical spectra SWSDW, shown as blue diamonds in Fig. 3(b). SWSDW is a measure of the itinerant part of the magnetic field in our samples, it can be inferred that this local magnetic field is due to nearby (on the scale of nanometers) magnetic moments. As we observe that \( \sim 100\% \) of the muons in the sample precess in a well-defined magnetic field, we conclude that \( \sim 100\% \) of the sample volume hosts ordered magnetic moments.

This issue is of importance given earlier results which showed a real-space phase separation in BKFA single crystals into magnetic and nonmagnetic regions [26,27,43,62]. Goko et al. reported a mixed volume fraction of magnetic and nonmagnetic regions, with approximately equal volume fraction, below 70 K and a sharp SC transition temperature at \( T_c = 32 \text{ K} \) [27]. These samples have a somewhat broad magnetic transition which might suggest a large distribution of K content in their samples. In contrast, Hiraishi et al. failed to see a magnetic volume fraction with ZF-μSR for their polycrystalline samples below 70 K and a sharp SC transition temperature at \( T_c = 32 \text{ K} \) [27].

A similar observation was made in Ref. [43]. These samples have a somewhat broad magnetic transition which might suggest a large distribution of K content in their samples. In contrast, Hiraishi et al. failed to see a magnetic volume fraction with ZF-μSR for their polycrystalline samples below 70 K and a sharp SC transition temperature at \( T_c = 32 \text{ K} \) [27].

B. Magnetic volume fraction: Phase separation?

For samples \( x \leq 0.26 \), the volume fraction of the magnetic state is, with experimental uncertainty, 100%. This was consistently determined from both ZF-μSR, where the fitted \( A_i \) give the magnetic volume fractions, and more directly from TF-μSR measurements at temperatures just above \( T_c \). The temperature dependence of the magnetic volume fraction for various \( x \) as determined by TF-μSR is shown in Fig. 4. In these measurements, if there were a nonmagnetic fraction it would result in a signal with a small relaxation rate \( \lambda \approx 0.2 \text{ µs}^{-1} \) at the frequency of the external field (below \( T_c \), SC vortices broaden and shift \( B_\mu \)). A full magnetic volume fraction in this doping regime was also reported by the μSR study of Ref. [8] on polycrystalline samples.

Note that magnetic stray fields in AF or SDW ordered states decay rapidly over a short range, on the order of a few nanometers, due to the mutual cancellation of the contribution from neighboring magnetic moments. Hence, if in a ZF-μSR measurement a muon spin is observed to precess in a local magnetic field in our samples, it can be inferred that this local magnetic field is due to nearby (on the scale of nanometers) magnetic moments. As we observe that \( \sim 100\% \) of the muons in the sample precess in a well-defined magnetic field, we conclude that \( \sim 100\% \) of the sample volume hosts ordered magnetic moments.

FIG. 4. The temperature dependence of the magnetic volume fraction determined from TF-μSR measurements for underdoped BKFA single crystals.
a doping state with intrinsic phase separation and possibly a qualitatively different relation between magnetism and SC. Such a scenario has been reported in BFCA [9]. We mentioned earlier that some of our own $x = 0.33$ crystals showed a partial magnetic volume fraction, and such a scenario appears to be consistent with the observations of Park et al. [27]. It is of great interest to study this region in more detail with $\mu$SR and fine control of sample quality will be key to this pursuit. This seems to mostly pertain to doping homogeneity, but there are possibly additional contributing factors such as crystal strain.

C. Coexistence of superconductivity and magnetism

Although a SC transition is seen at $T_c = 6$ K for the $x = 0.15$ sample, our $\mu$SR data do not provide proof that SC is a bulk phenomenon at this doping since we do not see characteristic SC anomalies below $T_c$. Similar observations were made by neutrons [63]. However, for all $0.19 \leq x \leq 0.26$ there is clear evidence of a coexistence and competition of superconducting and magnetic order on a nanometer scale.

The first set of evidence from $\mu$SR for this concerns the decrease in ZF and TF $\mu$SR frequency below $T_c$, as shown in the inset to Fig. 5 for ZF-$\mu$SR. A decrease in the magnetic order parameter below $T_c$ was also seen in polycrystalline BKFA with ZF-$\mu$SR for $x = 0.19$ and 0.23 [8] and by neutron diffraction experiments for polycrystalline BKFA with $x = 0.21$ [63]. The suppression of the magnetic order parameter concurrent with the onset of SC strongly suggests a coexistence and competition between the two orders. The second piece of evidence comes from so-called pinning experiments [Fig. 5(b)]. In this experiment, the sample is cooled in a moderate field, 20 mT, followed by a high-statistics $\mu$SR spectrum collected at low temperature. Next, without changing the temperature, the applied field is changed. If the magnetic flux density inside the sample remains unchanged, despite the change in externally applied field, it shows the existence of a bulk type-II SC state with pinned vortices whose volume fraction can be estimated from the data. We did not observe such a pinning effect for the $x = 0.15$ doping state at 1.5 K, it was observed in the other two samples tested, $x = 0.19$ and 0.23, signifying a bulk SC state at these doping levels. Results of the pinning experiment for $x = 0.19$ are shown in Fig. 5(b). Here, the sample was field cooled from $T > T_n$ in 20 mT to $T = 1.6$ K and a high-statistics spectrum collected. The four main peaks, shown in the inset to Fig. 5(b), correspond to the zero field $B_{\mu}$ at the main and secondary muon site (which is parallel to the $c$ axis [18]) split by $\pm 20$ mT, the applied field (that is also parallel to the $c$ axis). The field was then decreased by 5 mT and then a further 5 mT. A weak peak, indicated by the arrows and resulting from the small fraction of muons that stop outside of the sample, is seen to follow the external field, while the main features, due to the muons that stopped inside the sample, remain essentially unchanged.

Combined with the observation of a full magnetic-volume fraction shown in Fig. 4, these two observations show that SC and magnetism coexist on a nanoscopic scale and compete in underdoped BKFA.

The behavior for the $x = 0.43$ sample is different. First, as shown in Fig. 2, there are no observable oscillations, no fast relaxation and/or missing volume fractions in the ZF-$\mu$SR data at $T = 2$ K which indicates the absence of static magnetism. This is somewhat different to BFCA around optimal doping where a spatially inhomogeneous, static-magnetic state develops only below $T_c$ [9]. Instead, it is not until a more substantially overdoped Ba(Fe$_{1-x}$Co$_{0.11})_2$As$_2$ that static magnetism is no longer observed at any temperature. However, even here, it was found that spin fluctuations were enhanced below $T_c$. Thus, to investigate the magnetic state of our $x = 0.43$ BKFA sample further, we carried out a series of LF-$\mu$SR experiments for $H = 0.5$, 1, and 2 mT. In a weak LF, the small contribution to the relaxation rate from nuclear magnetic moments can be suppressed, so that a weak contribution of muon relaxation due to fluctuations can be resolved. The data were fitted to $P(t) = P(0)g(\nu_0,\sigma,t)e^{-\lambda t}$, where $e^{-\lambda t}$ is the contribution to the relaxation from spin fluctuations and $g(\nu_0,\sigma,t)$ is a standard expression describing

![FIG. 5. Coexistence of superconductivity and magnetism. (a) The temperature dependence of $B_{\mu}$ from ZF-$\mu$SR for several of the measured samples. (b) Results of a so-called pinning experiment for $x = 0.19$ revealing a pinned vortex lattice. The sample was field cooled in 20 mT to $T = 1.6$ K.](image-url)
the contribution from nuclear magnetic moments in a weak LF [64]. The full expression for $g(v_0,\sigma,t)$ is

$$g(v_0,\sigma,t) = 1 - \frac{2\sigma^2}{v_0^2} \left[ 1 - e^{-\frac{t}{2\gamma\mu\mu/2\pi}} \right] + \frac{2\sigma^4}{v_0^4} \int_0^t e^{-\frac{1}{2\gamma\mu\mu/2\pi} \sin(v_0 \tau) d\tau},$$

where $\sigma$ represents the distribution width of nuclear magnetic moment values and is approximately temperature independent. $\sigma = 0.1 \mu s^{-1}$ was determined by fitting the highest-temperature data and was then kept fixed for lower-temperature-data fits. $v_0 = \gamma_0 \mu_0 H_0/2\pi$ with $H_0$ the applied magnetic field (a fixed parameter in the fitting).

The results are shown in Fig. 6 and reveal that $\lambda^{LF}$ exhibits an anomalous increase below $T_c$. The effect is similar, though almost twice as large as that seen for the overdoped electron-doped sample with Ba(Fe$_{1-\delta}$Co$_{\delta}$)$_2$As$_2$ [9]. In our case, however, the field dependence of the change in $\lambda^{LF}$ at low temperature with respect to the normal state $\Delta \lambda^{LF}$ shown in the inset does not follow a Redfield functional form. The increase may be due to a gapping of scattering channels for spins in the SC state that gives rise to observable spin fluctuations below $T_c$, or a contribution from vortices that are not aligned with the external field (although in that case the size of the effect should scale with the vortex density and therefore the external field strength). On the other hand, the enhancement of spin fluctuations in the SC state might suggest a constructive rather than competitive relation between SC and magnetism for these doping states near the maximum of the $T_c$ dome. There is also the possibility that the enhanced relaxation is due to the SC state itself, i.e., from an exotic SC order parameter with a spin-triplet component as seen in Sr$_2$RuO$_4$ [65], PrOs$_2$Sb$_{12}$ [66], or LaNiC$_2$ [67].

Finally, for optimally doped to overdoped samples we do not see the paramagnetic shift in $B_{\mu\mu}$ below $T_c$ in TF-$\mu$SR experiments that was reported before in the electron-doped 122 compounds [9,44,46,68]. Instead, we see the more customary diamagnetic shift due to a screening of the magnetic field in the SC state (not shown). An estimate of the in-plane London penetration depth $\lambda_L$ was then calculated from the second moment of the real part of the Fourier transform of $P(t)$ after, for example, Refs. [69,70]. We find $\lambda_L \approx 200$ nm at $T = 5$ K for both our optimally doped and overdoped samples. Residual magnetic order and/or vortex lattice disorder in these samples introduces a systematic uncertainty in such an estimate of $\lambda_L$ based on TF-$\mu$SR measurements with a possible underestimation of $\lambda_L$ to some degree [68]. However, separate estimates of $\lambda_L$ based on our IR spectroscopy data for these samples, shown in Sec. IV C, also give a similar value of $\approx 200$ nm.

The exact Fermi-surface shape, Hund’s rule couplings, and disorder in these compounds are undoubtedly very important factors for the manifest electronic and magnetic properties. However, the similarity between BFCA and BKFA phenomenology shown here suggests that the (i) coexistence and competition of SC and magnetism in underdoped compounds and (ii) SC-enhanced magnetism in near optimal-doped and overdoped samples are effects intrinsic to BFA that rather relate to the proximity of magnetic and SC orders.

IV. OPTICAL SPECTROSCOPHY

To complement the $\mu$SR results presented above, we have also studied several of the samples with IR optical spectroscopy. Representative spectra for $x = 0.24$ of the reflectivity $R$ are shown in Fig. 7(a), with the corresponding spectra of the real part of the optical conductivity $\sigma_1$ presented in Fig. 7(b) and the real part of the dielectric function $\varepsilon_1$ in Fig. 7(c). Similarly, we show the response for the slightly overdoped sample with $x = 0.43$ in Figs. 7(d)–7(f).

A. Normal-state response

In the high-temperature paramagnetic state $T > T^N$, the spectra are similar to those previously reported in the literature [17,34–36,38,41,42,47,55,56]. They show a Drude response at low frequencies, arising from the itinerant carriers on the multiple bands crossing the Fermi energy. From the extrapolation of the Drude response to zero frequency we estimate the dc resistivity, which we find decreases at room temperature from $\rho_{dc} \approx 400 \mu \Omega \text{cm}$ for $x = 0$ to $\rho_{dc} \approx 250 \mu \Omega \text{cm}$ at higher $x$. These values are consistent with those previously reported in the literature for BKFA ($\rho_{dc} \approx 250$ to 400 $\mu \Omega \text{cm}$) [30,71]. Looking to higher frequencies, the Drude response exhibits a pronounced tail that results from inelastic scattering of the itinerant carriers [72]. At these frequencies there are also contributions from the low-energy interband transitions that are, for example, responsible for the upturn in $\sigma_1$ around 5000 cm$^{-1}$. With increasing $x$, they are expected to move to lower energy leading to a significantly larger fraction of the low-energy spectral weight arising from interband transitions [73], and our ellipsometry data support this prediction.

With decreasing $T$, the Drude response from at least one of the bands narrows and the spectral weight of the Drude terms decreases overall due to a transfer to high energies that originates from the strong Hund’s-rule coupling [35,55,74].
FIG. 7. Optical response of BKFA. (a) The far-infrared reflectivity for \( x = 0.24 \) at selected temperatures. The inset shows the reflectivity at low temperatures divided by the spectrum with \( T \approx T_c \). Dotted lines in panel (a) show the low-frequency extrapolations used, in conjunction with mid-infrared ellipsometry, to determine the corresponding real part of the optical conductivity \( \sigma_1 \), shown in panel (b), and real part of the dielectric function \( \epsilon_1 \), shown in panel (c). The insets to panels (b) and (c) show the room-temperature data to near-UV energies. Corresponding data are shown for \( x = 0.43 \) in panels (d)–(f).

Changes in the response from the low-energy interband transitions are much less pronounced. In this temperature regime, we do not see evidence for a collective mode at \( \approx 150 \text{ cm}^{-1} \) as was observed in Ref. [39]. A low-frequency feature at \( \approx 120 \text{ cm}^{-1} \) developing below a certain temperature \( T^* \) has also been reported in underdoped BKFA samples with \( x \approx 0.30 \) (\( T_c = 36 \text{ K} \), \( T^N \approx 100 \text{ K} \)) at \( T^* \approx 100 \text{ K} \) by Kwon et al. [40], and with \( x = 0.20 \) (\( T_c = 19 \text{ K} \) and \( T^N = 104 \text{ K} \)) and, less prominently, \( x = 0.12 \) (\( T_c = 11 \text{ K} \) and \( T^N = 121 \text{ K} \)) [42]. It is difficult to distinguish a similar feature in our raw data. We performed a similar spectral weight analysis to Ref. [42] in order to estimate \( T^* \) in our own samples. For \( x = 0.23 \) and 0.24, \( \sigma_1 \) of \( T^* \) we observe are approximately coincident with \( T_c \) making it difficult to distinguish from an effect relating to the formation of a SC gap. For \( x = 0.19 \), \( T^* \) may be up to 40 K, which, while somewhat below the 80 K found in Ref. [42] for \( x = 0.20 \), is still somewhat higher than \( T_c = 15 \text{ K} \) for this sample.

The IR-active phonon mode observable near 260 cm\(^{-1}\) corresponds to the in-plane vibrations of Fe against As [55,75,76] and generally displays only a weak temperature dependence and a weak dependence on \( x \). The second expected IR-active mode around 95 cm\(^{-1}\), which is dominated by the displacement of Ba, is not resolved for \( x > 0 \) samples, most likely due to the disorder from the K substitution.

**B. Signatures of magnetic order in the IR response**

For the underdoped samples, in the magnetic state the optical response undergoes significant changes that stem from a partial gapping of the Fermi surface due to the formation of a spin-density wave (SDW). These are a peak around 800 cm\(^{-1}\) in \( \sigma_1 \) corresponding to the SDW pair-breaking peak and a reduction of the spectral weight of the Drude response [34,47,55,56]. Figure 8(a) highlights the temperature evolution of the SDW in \( \sigma_1(T) \) for \( x = 0.23 \) as an example. The evolution is characterized by a progressive redistribution of spectral weight from lower energies, seen for example in Figs. 7(b) and 7(c) by the suppressed conductivity around 400 cm\(^{-1}\) and corresponding peak in \( \epsilon_1 \), to higher energies to form a characteristic pair-breaking peak in \( \sigma_1 \). These features grow relatively rapidly below the \( T^N \) determined by \( \mu \Sigma R \) (100 K in this case) and then display little change below 50 K. The peak center in \( \sigma_1 \) moves only slightly from \( \approx 700 \text{ cm}^{-1} \) just below \( T^N \) to \( \approx 850 \text{ cm}^{-1} \) at low temperature.

The \( x = 0 \) and 0.26 samples have qualitatively different behavior from that described above. For \( x = 0 \), this concerns an additional SDW feature peaked at a lower energy [34,47] of about 400 cm\(^{-1}\). For \( x = 0.26 \), in the t-AF phase a distinct SDW is observed in the temperature range 32 K \( \approx T^{N2} > T > T^{N3} \approx 18 \text{ K} \) with a reentrance of the o-AF state below \( T^{N3} \) [17,28,33]. This can be seen in Fig. 9 which shows the temperature dependence of \( \sigma_1 \) for \( x = 0.26 \) in the vicinity of the o-AF to t-AF transitions [17]. Note that in Fig. 10(b), data for \( x = 0.26 \) in the o-AF state are shown.

Signatures of a SDW state in the optical response, at any temperature, disappear between \( x = 0.26 \) and 0.30. This is consistent with the results from Böhmer et al. that show no lattice distortions associated with magnetism above \( x \approx 0.28 \) [28].

The SW of the pair-breaking peak reflects the magnitude of the order parameter of the SDW and thus of the ordered magnetic moment due to the itinerant carriers. Our procedure
FIG. 8. Spin-density-wave (SDW) feature in the optical response of $x = 0.23$. (a) The temperature dependence of the SDW absorption as seen in $\sigma_1$. (b) The fitting procedure used to estimate the SW of the SDW corresponding to the filled green area. The red points show the 150-K data. The black solid line is the corresponding fit with the light gray lines showing the Drude and Lorentzian components of the fit. Similarly, the blue points are the 30-K data with the green lines the total fit and fit components. (c) The estimated $SW_{SWD}$ as a function of temperature. Blue symbols show the magnetic field at the muon site $B_\mu$ from ZF-$\mu$SR.

for estimating the SW associated with the SDW as follows: we first fit the “normal-state” (i.e., $T > T^N$) $\sigma = \sigma_1 + i\sigma_2$ for $x = 0.23$ at $T = 30$ K showing the evolution of the SDW with doping $x$.

FIG. 9. The SDW feature in the optical response of $x = 0.26$ has a distinct shape in t-AF phase, which occurs in the temperature range $32 \: K \approx T^{N2} > T > T^{N3} \approx 18 \: K$. Below $T^{N3}$, there is a reentrance of the o-AF state.

data between 0 and 4000 cm$^{-1}$ using two Drude terms and three broad Lorentzian oscillators (representing the interband transitions). Such a fit is shown in Fig. 8(b) for $x = 0.23$ at $T = 30$ K showing the evolution of the SDW with doping $x$. (b) The fitted SDW from the data in (a) using the procedure outlined in the text and Fig. 8(b).
150 K. Fitting the data below $T^N$, we keep the Lorentzian oscillators fitted from the data above $T^N$ essentially fixed (allowing only for small changes of the oscillator strength). The remainder of the spectrum is fitted by varying the Drude terms (which determine the low-frequency response) and introducing Gaussian oscillators to fit the pair-breaking peak. Gaussian oscillators are used because they are more localized than Lorentz oscillators and still give a phenomenological description of the data. The SW of the pair-breaking peak is then determined from the fitted Gaussian oscillators. While the absolute values obtained from this procedure are somewhat sensitive to the fitting model, they do provide a meaningful measure of the $x$ and $T$ dependencies since the same fitting models are used for all $x$.

By way of example, in Fig. 8(c) we show the $T$ dependence of the spectral weight of the pair-breaking peak, $SW_{SDW}$, for $x = 0.23$ estimated using the procedure above (red squares). Another measurable quantity related to the magnitude of the magnetic order parameter is the size of the magnetic moment, which is in turn related to the magnitude of the magnetic field at the muon site $B_\mu$. The temperature dependence of $B_\mu$, as measured by ZF-$\mu$SR for the main muon site is also plotted in Fig. 8(c) (blue circles) and shows a similar temperature evolution to the SW of the pair-breaking peak.

Figures 10(a) and 10(b) show raw data and fitted Gaussian oscillators for each $x$ at low temperature, $T_c < T < T^N$, respectively. With increasing $x$ the feature progressively moves to lower energy while its SW, a measure of the itinerant density means that there are fewer states available for the SC state. These estimates are in reasonable agreement with the temperature dependencies since the same fitting procedure is used at low $T$.

By means of the above fitting procedure and from a spectral-weight analysis of the raw data, we also estimate a SDW-induced decrease of the Drude weight of about 65% for the undoped $x = 0$ sample to 35% ± 10% for $x = 0.20$ and falling to about 25% ± 10% for $x = 0.26$ (in the $\alpha$-AF state). These estimates are in reasonable agreement with the heat-capacity data [77]. This reduction in the itinerant carrier density means that there are fewer states available for the SC state.

Meanwhile, the energy of the feature $E_{SDW}$, that we estimate from the peak in $\sigma_1$ in Fig. 10(b), moves slightly lower with $x$, from $E_{SDW} \approx 950$ cm$^{-1}$ (120 meV) for $x = 0$ to about 800 cm$^{-1}$ at $x = 0.26$. This suggests a lower-energy SDW-related gapping of the Fermi surface. Within uncertainties, however, the ratio $2E_{SDW}/T^N$ remains 5.0 ± 0.5 across the underdoped samples, where $T^N$ has been taken from the $\mu$SR data. We note that signatures of the SDW state in the optical data are evident between 10 and 30 K higher than $T^N$ across the underdoped series. This is probably related to predicted fluctuations of the SDW [13] above the frequency probed by the experimental techniques (THz in IR spectroscopy compared with MHz for $\mu$SR) [17,47]. A very recent optical study of underdoped BKFA also notes signatures of the SDW above the $T^N$ found from static probes [78]. Going further, at the fast, sub-fs time scales probed with x-ray emission spectroscopy, a significant Fe magnetic moment is observed at room temperature [19].

These observations paint the picture of a SDW of relatively constant energy scale, but which gains a progressively smaller area of the Fermi surface as $x$ increases and which rather abruptly disappears above $x \approx 0.28$.

C. Superconductivity

The pnictides are by now well known for the microscopic coexistence of superconducting and magnetic phases that they exhibit and, as shown by the $\mu$SR data, underdoped BKFA is no exception. Optical spectroscopy was able to show early on that these two phases compete in the underdoped regime for the same electronic states [6], whereby the SW of the SDW decreased at the onset of SC. Although such a decrease was not clearly seen in our BKFA data, the optical data presented here do show a similar phenomenology for BKFA in that the SC gap energy and superfluid density are enhanced in the absence of a SDW state.

At low energy and temperature, $R = 1$ with experimental uncertainties for $x \geq 0.19$ implying a bulk, nodeless superconducting state. In conjunction with the $\mu$SR results on the same samples which showed a 100% magnetic volume fraction, we can confirm the bulk coexistence of SC and magnetic states (in real space) in BKFA. It has been shown previously that more than one SC gap is evident from the optical spectra of BKFA [36,39] and our data are consistent with this multigap scenario. A detailed analysis of the gap shape is a subject beyond the scope of this work and would likely provide more robust low-frequency extrapolations of the reflectivity data.

We find evidence that the shape of the SC gap appears to change between $x = 0.24$ and 0.33 as shown in Figs. 7(a) and 7(d) and in Fig. 11.

The insets to Figs. 7(a) and 7(d) show the reflectivity ratio for a magnetic $x = 0.24$ sample and a nonmagnetic $x = 0.43$ sample. The reflectivity edge in the SC state is clearly much more pronounced in the nonmagnetic sample, occurs at higher energy, and grows rapidly immediately below $T_c$. Figure 11(a) shows $\sigma_1$ immediately above $T_c$ and at $T = 7$ K for three samples which span this transition. For $x = 0.24$, a significant redistribution of SW from the normal state to the SC state extends only up to 140 cm$^{-1}$ in energy. At the slightly higher doping of $x = 0.26$, it is up to 440 cm$^{-1}$ and by $x = 0.33$ up to 725 cm$^{-1}$. Similarly, the steep decrease in $\sigma_1$ at low $T$ due to SC occurs at 100 cm$^{-1}$ for $x = 0.24$ and increases to 345 cm$^{-1}$ for $x = 0.33$.

Using the methodology outlined in Ref. [17] and references therein, we estimate the (in-plane) SC superfluid density $n_{SC}$ from $\epsilon_1$ and from the missing SW in $\sigma_1$. Figure 11(b) shows the doping dependence of the square of the SC condensate density plasma frequency $\omega_{pl,SC}$, which is proportional to $n_{SC}$ and $\lambda_{L}^{-2}$, as $\lambda_{L} = 1.61 \times 10^6/\omega_{pl,SC}$ (with $\lambda_{L}$ in nm and $\omega_{pl,SC}$ in cm$^{-1}$). There is a pronounced decrease in $n_{SC}$ for $x \leq 0.3$, coincident with the appearance of the SDW signatures in the optical response, a phenomenology that is similar to what is found in the cuprates with the opening of the pseudogap. This decrease in $n_{SC}$ also coincides with a decrease in the energy
of the largest superconducting gap $\Delta_p$ as determined from specific-heat measurements [25,77] and shown as red squares in Fig. 11(b). $n_{SC}$ changes little between our $x = 0.33$ and 0.47 with values consistent with those previously reported [36,39,45]. The derived in-plane London penetration depth is $\lambda_L \approx 200$ nm. This is in agreement with the values of $\lambda_L$ obtained from the TF-$\mu$SR data, which are shown as blue triangles in Fig. 11(b) for optimally and slightly overdoped samples. Static magnetic order in the underdoped samples prevents us from estimating $\lambda_L$ from the $\mu$SR data there.

A maximum in $n_{SC}$ for $x \approx 0.4$ has been reported from thermodynamic probes on BKFA [25,28,77]. In BFCA [9,25] and BNFA [29], a maximum in $n_{SC}$ has also been observed close to the point at which magnetism is no longer observable. For the case of BaFe$_2$As$_2$-2P$_2$ (BFAP), there are reports of a different behavior with a sharp minimum in the SC condensate density close to where magnetism disappears and the observation of nodes in the SC gap [79,80]. This apparent qualitative difference between BFAP and the electronically doped BKFA (and BFCA) is intriguing, and is unrelated to disorder since BKFA is a similarly “clean” from electronic disorder associated with the dopant. Measurements of $\lambda_L$ in BKFA between $x = 0.26$ and 0.5 in a finer mesh are desirable to test for any such increase in $\lambda_L$ in a narrow range of $x$.

Without a full multiband analysis of the gap shape, it is difficult to estimate the ratio $\Delta_{SC}/k_B T_c$. Although, considering the similarity of our data to Ref. [39], a ratio of about 6 for at least one of the bands is not inconsistent.

V. SUMMARY

In underdoped BKFA, we find a concomitant decrease in local magnetic field from the Fe moment as measured by $\mu$SR, $B_{\mu}$, and the spectral weight of the spin-density-wave feature $SW_{SDW}$ in the IR-optical response. On increasing the doping, $B_{\mu}$ initially decreases more slowly than the Néel temperature until it too falls rapidly close to optimal doping. A comparison of the evolution in doping of $B_{\mu}$ and $SW_{SDW}$ suggests that close to optimal doping, where the static magnetic order disappears sharply, the itinerant magnetic moment decreases even faster than the total magnetic moment. In the overdoped samples, there is no evidence of a static magnetic order.

In the moderately underdoped region, we see a coexistence of static antiferromagnetic magnetic order and superconductivity on a nanoscopic scale. Here, the two orders compete for the same electronic states as shown by (i) the reduced magnetic order parameter below $T_c$ from $\mu$SR, (ii) the optical conductivity showing a capture of spectral weight by the spin-density wave from the low-frequency Drude response (spectral weight that could otherwise contribute to the SC condensate), and (iii) the marked increased in the superconducting gap energy and condensate density between the slightly underdoped and optimally doped samples. In the slightly overdoped region, however, where the optical response shows a strong superconducting state, our LF-$\mu$SR data suggest a qualitatively different relation between superconductivity and magnetism whereby spin fluctuations are enhanced below $T_c$. A similar observation has been made in the electron-doped system BFCA [9].

We consider it possible that around optimal doping, yet more novel electronic/magnetic properties might be discovered. This is partly suggested by the novel t-AF magnetic state in BKFA with a doping state of $x = 0.26$ [18,30–33] and by our observation here of spin fluctuations below $T_c$ in slightly overdoped samples. Specific-heat and thermal expansion on BKFA point to a rich competition of phases in this doping regime [25,28], and it would be interesting to study in detail using the more sensitive magnetic probe of $\mu$SR. More recently, a similar specific-heat and thermal-expansion study of Ba$_{1-x}$Na$_x$Fe$_2$As$_2$ indeed showed novel magnetic states as the Néel temperature approaches the value of $T_c$ [29]. BaFe$_2$As$_2$ is apparently host to several near-degenerate magnetic states whose energy depends on parameters such as bond lengths, impurity scattering, and Fermi-surface nesting. The similarities between the BFCA and BKFA phenomenology shown here may help to elucidate the role of each of these parameters.
ACKNOWLEDGMENTS

This work was supported by the Schweizerische Nationalfonds (SNF) through Grant No. 200020-153660 and the Marsden Fund of New Zealand. Some measurements were performed at the IR beam line of the ANKA synchrotron at FZ Karlsruhe, where we acknowledge the support of Y. L. Mathis and M. Säpfle. We thank C. Neururer and B. Grobety for the electron dispersion spectroscopy measurements. The μSR work has been performed at the Swiss Muon Source at the Paul Scherrer Institute, Switzerland.
