X-ray absorption spectroscopy study of the electronic and magnetic proximity effects in YBa$_2$Cu$_3$O$_7$/La$_2$/Ca$_{1}$/MnO$_3$ and La$_2$-xSr$_x$CuO$_4$/La$_2$/Ca$_{1}$/MnO$_3$ multilayers

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With x-ray absorption spectroscopy we investigated the orbital reconstruction and the induced ferromagnetic moment of the interfacial Cu atoms in YBa$_2$Cu$_3$O$_7$/La$_2$/Ca$_{1}$/MnO$_3$ (YBCO/LCMO) and La$_2$-xSr$_x$CuO$_4$/La$_2$/Ca$_{1}$/MnO$_3$ (LSCO/LCMO) multilayers. We demonstrate that these electronic and magnetic proximity effects are coupled and are common to these cuprate/manganite multilayers. Moreover, we show that they are closely linked to a specific interface termination with a direct Cu-O-Mn bond. We furthermore show that the intrinsic hole doping of the cuprate layers and the local strain due to the lattice mismatch between the cuprate and manganite layers are not of primary importance. These findings underline the central role of the covalent bonding at the cuprate/manganite interface in defining the spin-electronic properties.

I. INTRODUCTION

The new phenomena that arise when different interactions and orders meet at the interfaces of multilayers (MLs) from complex oxides with strongly correlated electrons are of great current interest [1]. The versatile properties of the complex oxides provide many opportunities, but they make it also very challenging to identify the underlying principles and interactions.

A prominent example are MLs from cuprate high-$T_C$ superconductors and ferromagnetic (FM) manganites. They have appealing properties, like the high superconducting (SC) critical temperatures, $T_C$, of the cuprates and the nearly 100% spin polarized charge carriers of the manganites. Studies on YBa$_2$Cu$_3$O$_7$/La$_2$/Ca$_{1}$/MnO$_3$ (YBCO/LCMO) MLs have already provided evidence for a giant magnetoresistance effect [2], a giant superconductivity induced change of the ferromagnetic order [3], and a proximity-induced spin-triplet SC state [4,5]. The latter is a well-established phenomenon in conventional SC/FM MLs where it requires a specific magnetic structure with a noncollinear order near the interface [6–8].

The corresponding magnetic properties of the cuprate/manganite MLs remain to be understood. The YBCO/LCMO MLs have been shown to exhibit an unusual magnetic proximity effect (MPE) that involves a suppression of the FM order of the Mn moments on the LCMO side of the interface [9–11] and, yet, an induced FM moment of the Cu atoms on the YBCO side. The latter has been established with Cu L-edge x-ray magnetic circular dichroism (XMCD) studies [10,12,13]. Notably, these Cu moments are antiparallel with respect to the Mn moments. A subsequent x-ray linear dichroism (XLD) study suggested that an orbital reconstruction of the interfacial Cu atoms and a charge transfer across the interface are at the heart of this MPE [14]. The orbital reconstruction, the charge transfer, and the antiferromagnetic (AF) coupling between Cu and Mn moments have been explained in terms of a covalent bonding of Cu and Mn via the apical oxygen, O° [14]. This covalent bonding model relies on the specific interface termination of these YBCO/LCMO MLs with a CuO$_2$-BaO-MnO$_2$ layer stacking which has been observed with high-resolution transmission electron microscopy (HRTEM) [15,16].

The relevance of the covalent bonding model and, in particular, how these electronic and magnetic proximity effects depend on the interface termination, on the local strain and related defects and on the hole doping and thus the strength of the magnetic correlations of the cuprate layers need to be explored. This is especially important since subsequent experimental and theoretical studies on YBCO/LCMO MLs yielded controversial results which question the direct relationship between the orbital reconstruction and the induced Cu moments [17,18].

In this paper, we present a combined XLD and XMCD study on YBa$_2$Cu$_3$O$_7$/La$_2$/Ca$_{1}$/MnO$_3$ (YBCO/LCMO) and La$_2$-xSr$_x$CuO$_4$/La$_2$/Ca$_{1}$/MnO$_3$ (LSCO/LCMO) MLs, which establishes a direct relationship between the orbital reconstruction and the induced FM moment of the interfacial Cu atoms and underlines the important role of the interface termination. The unique properties of the LSCO/LCMO system also allow us to vary the hole doping of the CuO$_2$ planes and to explore the role of the local strain due to the lattice mismatch between the cuprate and manganite layers.

II. EXPERIMENTAL

The pulsed laser deposition (PLD) growth of the LSCO/LCMO [10 nm/10 nm]$_{9}$ and [8.5 nm/8.5 nm]$_{1}$ (9 BL and 3 BL) MLs on SrLaAlO$_4$ (SLAO) substrates has been reported in Ref. [19]. The one of a corresponding YBCO/LCMO
[10 nm/10 nm]_{10} ML on La$_{0.3}$Sr$_{0.7}$Al$_{0.65}$Ta$_{0.35}$O$_3$ (LSAT) in Ref. [16].

The XMCD and XLD studies were performed at the XTreme beamline at the Swiss Synchrotron Light Source (SLS) of Paul Scherrer Institute (PSI) in Villigen, Switzerland [20]. Additional measurements (not shown) were done at the WERA beamline of the ANKA synchrotron at K.I.T., Germany. The x-ray absorption spectroscopy (XAS) curves were measured at the Mn and Cu-$L_{3,2}$ edges using the total electron yield (TEY) and total fluorescence yield (FY) modes. The data have been normalized and background-corrected following the procedure detailed in Appendix A.

For XLD, the absorption for $\sigma$ and $\pi$ linear polarization was measured with an angle of incidence of 15° for YBCO/LCMO and LSCO/LCMO 9 BL and 20° for LSCO/LCMO 3 BL. The absorption for polarization parallel to the planes, $\mu_{ab}$, is directly obtained from the $\sigma$ polarization measurement. To obtain the absorption for the out-of-plane polarization, $\mu_c$, the measurement geometry needs to be considered since in $\pi$ polarization the electric field has finite in-plane and out-of-plane components. As a function of the incidence angle with respect to the sample surface, $\theta$, the absorption for $\pi$ polarization yields [21] $\mu_c = \mu_{ab} \sin^2 \theta + \mu_c \cos^2 \theta$. The value of $\mu_c$ can thus be calculated as

$$\mu_c = \frac{\mu_{ab} - \mu_c \cos^2 \theta}{\sin^2 \theta}. \quad (1)$$

For XMCD, the absorption for circular polarization with positive and negative helicity, $\mu_+$ and $\mu_-$, was measured with the same incidence angles as for XLD. The magnetization was always first saturated at 3 T before the XMCD was measured at 0.5 T applied along the direction of the incident x rays. The dichroism has been obtained by switching both the direction of the applied field and the x-ray polarization to avoid experimental artifacts.

### III. RESULTS AND DISCUSSION

Figures 1 and 2 compare the Cu $L$-edge XAS curves, measured in the FY and TEY modes with linear and circular polarization, of the YBCO/LCMO and LSCO/LCMO MLs, respectively. They show that both MLs exhibit clear signatures of an orbital reconstruction and an induced FM moment of the interfacial Cu atoms. For the following discussion, it is important to recall that the TEY mode has a very small probe depth of only a few nanometers, which is limited by the escape depth of the photoelectrons. The TEY signal is thus governed by the response of the Cu atoms at the topmost cuprate/LCMO interface. The FY mode has a much larger probe depth of about 100 nm and thus yields an averaged response of the Cu atoms in several cuprate layers.

The orbital reconstruction of the interfacial Cu atoms is evident from the different polarization dependence of the XAS curves in FY and TEY mode in Figs. 1(a)–1(d) for YBCO/LCMO and 2(a)–2(d) for LSCO/LCMO. The FY curves yield a strong dependence of the absorption on the polarization direction that is characteristic of the bulk cuprates. Due to the predominant $d_{xy}$ character of the Cu holes in the CuO$_2$ layers, the absorption peaks at the Cu-$L_{3,2}$ edges are much more intense for the in-plane polarization [22,23]. This so-called XLD effect is much weaker in the TEY curves for which the absorption peaks for the out-of-plane polarization also exhibit a sizable intensity. This observation suggests that for the Cu atoms at the topmost interface the holes are more equally distributed between the $d_{x^2−y^2}$ and $d_{3z^2−r^2}$ levels. This orbital reconstruction was previously reported for YBCO/LCMO [14], our new data show that it occurs equally well for LSCO/LCMO and thus is common to the cuprate/manganite MLs.

A quantitative analysis of the electric and magnetic properties of the Cu atoms at the interface has been carried out by means of a multicomponent peak fit of the absorption spectra in the region around the Cu-$L_3$ edge. The resonant signal has been

**FIG. 1.** (Color online) XAS curves at the Cu-$L_{3,2}$ edge of YBCO/LCMO taken at 2 K. (a) XAS data for linear polarization in FY mode. (b) Close-up of the $L_3$ edge. Data (points) are shown together with the fit (thick lines) using four Lorentzian functions (thin lines) and a background with a linear and a sigmoid function (thin black line). The XLD of each peak is indicated by the patterns. (c) and (d) Corresponding XAS data for linear polarization in TEY mode. (e) and (f) XAS and XMCD data for circular polarization in TEY mode. (g) and (h) Corresponding XAS and XMCD data for circular polarization in TEY mode.
The multiplet fitting of the absorption peaks at the L edge shown in Figs. 1(b), 1(d), 1(f), and 1(h) reveals a clear substructure that is similar for the YBCO/LCMO and LSCO/LCMO MLs. In the former, it consists of four subpeaks at about 930.5, 931, 931.6, and 932.8 eV.

The other peaks can be assigned to Cu atoms away from the interface or to CuO chains. In the latter, they have a higher concentration and a strong out-of-plane character [23]. This explains the similar intensity of the in-plane and out-of-plane absorption of the peaks at 931.6 and 932.8 eV.

Notably, the XAS curves of the LSCO/LCMO ML in Figs. 2(b), 2(d), 2(f), and 2(h) show a corresponding low-energy peak at 930.5 eV that is also much stronger in TEY than in FY mode and thus can be assigned to the Cu atoms at the YBCO/LCMO interfaces. The orbital reconstruction of these atoms is confirmed by the reduced difference between the in-plane and out-of-plane polarization as compared with the bulk behavior. The fact that the absorption intensity for the in-plane polarization is still larger than the out-of-plane suggests that the so-called “Zhang-Rice singlet” in the CuO2 planes and the edge jumps in the vicinity of the absorption edge are orbitally reconstructed and their holes have a predominant d_{3z^2-r^2} character.

The other peaks can be assigned to Cu atoms away from the interface since they are stronger in FY mode and similar peaks occur in bulk YBCO [23]. The peak at 931 eV corresponds to the 2p^6 3d^9 2p^5 4f^{10} transition. As already mentioned, the absorption intensity of this peak for the out-of-plane polarization is small due to the predominant in-plane character of holes in the CuO2 planes. The other two peaks have been assigned to 2p^6 3d^9 L → 2p^5 d^{10} L transitions, where L denotes a hole on the oxygen ligand. Their higher energy arises from the Coulomb repulsion due to the overlap between the core hole and the oxygen ligand hole. The 3d^{10} L state corresponds to the so-called “Zhang-Rice singlet” in the CuO2 planes and CuO chains. In the latter, they have a higher concentration and a strong out-of-plane character [23]. This explains the similar intensity of the in-plane and out-of-plane absorption of the peaks at 931.6 and 932.8 eV.

The multiplet fitting of the absorption peaks at the L edge has been constrained to a common value that was however allowed to vary between the FY and TEY curves.

The polarization-averaged normalized weight, \((2\mu_{ab} + \mu_{c})/3\), of the peaks contributing to the Cu-L edge absorption in FY and TEY modes. The peaks are labeled from lowest to highest energy. All the values are given in percentages.

<table>
<thead>
<tr>
<th>Peak Mode</th>
<th>YBCO/LCMO 9_BL</th>
<th>LSCO/LCMO 9_BL</th>
<th>LSCO/LCMO 3_BL</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 FY</td>
<td>4.7(7)</td>
<td>1.9(7)</td>
<td>–</td>
</tr>
<tr>
<td>TEY</td>
<td>41(3)</td>
<td>48(5)</td>
<td>14(1)</td>
</tr>
<tr>
<td>2 FY</td>
<td>45(2)</td>
<td>73(3)</td>
<td>–</td>
</tr>
<tr>
<td>TEY</td>
<td>37(4)</td>
<td>39(5)</td>
<td>62(4)</td>
</tr>
<tr>
<td>3 FY</td>
<td>20(2)</td>
<td>25(3)</td>
<td>–</td>
</tr>
<tr>
<td>TEY</td>
<td>8(2)</td>
<td>13(8)</td>
<td>24(3)</td>
</tr>
<tr>
<td>4 FY</td>
<td>31(3)</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>TEY</td>
<td>15(4)</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>
A significant difference between the YBCO/LCMO and LSCO/LCMO MLs concerns the fraction of orbitally reconstructed Cu atoms at the interface. Based on the thickness of the layers and the c-axis lattice parameters of YBCO and LSCO [16,19], it can be estimated that the Cu atoms at the interface in the YBCO/LCMO and LSCO/LCMO MLs correspond to 8% and 13% of the total, respectively. In contrast, the weight of the 930.5 eV peak in the FY curves amounts to about 4.7% and 2%, respectively (see Table I). While the absolute value of \( w \) should be considered with care, since it depends on the normalization and the background subtraction, the relative difference is still meaningful. It indicates that the fraction of orbitally reconstructed interfacial Cu atoms in LSCO/LCMO is significantly smaller than in YBCO/LCMO. This can indeed be understood in terms of the different interface termination. For YBCO/LCMO the top and bottom interfaces are reported to undergo the orbital reconstruction and the induced FM in Cu becomes evident from the close-up of the absorption curves at the \( L_3 \) edge. The fits of the XAS curves for YBCO/LCMO in Figs. 1(f) and 1(h) and for LSCO/LCMO in Figs. 2(f), 2(h), and 3(d) show indeed that only the low-energy peak at 930.5 eV exhibits a sizable XMCD. This important finding highlights that the FM moment originates from the very same Cu atoms which undergo the orbital reconstruction. A direct link between the electronic and magnetic proximity effects is thus confirmed. The sign of the XMCD signal is the same for LSCO/LCMO and YBCO/LCMO and indicates that the Cu moments are always antiparallel to the Mn moments.

Since the FM order of the Cu atoms is confined to the interface the fraction of probed FM Cu atoms in a XMCD experiment is generally unknown. Therefore an accurate determination of their magnetization is commonly elusive [12,17]. This difficulty is solved by the multiplet fitting analysis introduced in this paper. Since only the orbitally reconstructed atoms are magnetic, their fraction corresponds to the weight of the 930.5 eV peak in the polarization averaged absorption shown in Table I. After performing the sum rule analysis described in Ref. [26] and a subsequent normalization to the fraction of orbitally reconstructed atoms we obtain the Cu magnetization values shown in Table II. Notably, although the number of magnetic Cu atoms differs between these YBCO/LCMO and LSCO/LCMO MLs the magnetic moment does not exhibit a significant variation. Table II also shows the calculated moment obtained from the XMCD measurements in TEY mode performed at the Mn-\( L_{1,3} \) edge (spectra are not shown). They confirm that the topmost LCMO layers of the YBCO/LCMO and LSCO/LCMO MLs exhibit a sizable FM order.
We also explored the role of the hole doping of the CuO$_2$ planes and thus of the strength of the antiferromagnetic (AF) correlations that are intrinsic to the cuprate layers. In YBCO it is controlled by the oxygen content of the CuO$_2$ chains, which act as charge reservoirs for the CuO$_2$ planes and at full oxygenation yield an optimally doped state ($p \approx 0.15$) with maximal $T_c$. However, according to HRTEM studies, the CuO$_2$ planes next to the interface are lacking the neighboring CuO chain layer and thus may be strongly underdoped with static Cu moments and strong, intrinsic AF correlations. According to Refs. [14,15] the hole doping of the interfacial CuO$_2$ planes may be further reduced by a transfer of electrons from the manganite to the cuprate layers. In contrast, the LSCO/LCMO system allows one to determine and vary the intrinsic doping of the interfacial CuO$_2$ planes via the Sr substitution. Accordingly, we investigated additional LSCO/LCMO MLs with $x = 0$ and 0.3 for which the intrinsic doping yields an undoped state with long-range AF order or a strongly overdoped and essentially non magnetic state, respectively. Notably, as presented in Table III our XMCD data (spectra are not shown) reveal that the magnitude of the FM moment per orbitally reconstructed Cu atom is almost independent of the Sr content and thus hardly depends on the intrinsic doping and the strength of the intrinsic AF correlations of the cuprate layers. This confirms that this MPE is governed by the exchange coupling due to the local covalent bonding between the Cu and Mn atoms and the possibly related transfer of electrons from the manganite to the cuprate layers.

Finally, the comparison of LSCO/LCMO and YBCO/LCMO allowed us to explore the role of the local strain at the interface and subsequent defects. This is due to the different mismatch of the in-plane lattice parameters which amounts to about 2.5% between LSCO and LCMO [19] and 0.5% between YBCO and LCMO [16]. The similar behavior of the LSCO/LCMO and YBCO/LCMO MLs as discussed above suggests that the orbital reconstruction and the induced FM moment of the interfacial Cu atoms are not strongly affected by these strain effects. Nevertheless, the strength of the orbital reconstruction is somewhat larger in YBCO/LCMO than in LSCO/LCMO. These observations should motivate calculations based on the covalent bonding model of Ref. [14] to detail the relationship of the orbital reconstruction with the splitting and the relative shift of the $e_g$ levels of the interfacial Cu and Mn atoms and with the displacement of the apical oxygen along the Cu-O$^{2-}$-Mn bond [18]. A related effect that deserves further theoretical attention involves the broader peaks above 935 eV which according to Ref. [22] originate from transitions into hybridized Cu-$4s$ and Cu-$3d_{3z^2-r^2}$ levels. Figures 1(a), 1(c), 2(a), and 2(c) show that these are considerably weaker in the TEY than in FY curves, which suggests a modification of the local structure around the interfacial Cu atoms, due for example to a change of the Jahn-Teller distortion or the buckling of the CuO$_2$ planes. Such distortions may provide a complementary or alternative explanation for the redshift of the 930.5 eV peak that was previously interpreted in terms of an electron transfer from the manganite to the cuprate layers.

IV. CONCLUSIONS

In summary, with x-ray absorption spectroscopy on LSCO/LCMO and YBCO/LCMO multilayers, we have shown that the orbital reconstruction and the induced ferromagnetic moment of the interfacial Cu atoms are common to these cuprate/manganite multilayers. We have also established a direct link between these electronic and magnetic interface phenomena and we have shown that they require a specific kind of interface termination. The intrinsic hole doping of the cuprates and the local strain due to the lattice mismatch between the different layers is found to be less important. Our findings support the covalent bonding model [14] and related models [27–29]. They also highlight the important role of the interface termination in defining the spin-electronic properties of these oxide multilayers.

ACKNOWLEDGMENTS

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APPENDIX A: NORMALIZATION AND BACKGROUND SUBTRACTION OF THE TEY AND FY ABSORPTION CURVES

To single out the resonant part of the absorption due to the Cu-$L_{3,2}$ edges, it was necessary to subtract a background

| TABLE II. Calculated Cu and Mn spin magnetic moments of the YBCO/LCMO and LSCO/LCMO MLs. The values are calculated applying the sum rules to the TEY XMCD data at the Cu and Mn-$L_{3,2}$ edges. The nonresonant background in the XAS curves has been subtracted using the approach described in Ref. [26].

<table>
<thead>
<tr>
<th></th>
<th>YBCO/LCMO</th>
<th>LSCO/LCMO</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_{Cu}^{int} (\mu_B)$</td>
<td>$-0.18(4)$</td>
<td>$-0.16(4)$</td>
</tr>
<tr>
<td>$m_{Mn}^{int} (\mu_B)$</td>
<td>$1.7(3)$</td>
<td>$2.0(4)$</td>
</tr>
</tbody>
</table>

TABLE III. Calculated spin magnetic moment, in $\mu_B$, per orbitally reconstructed Cu atom for the LSCO/LCMO multilayers with different Sr doping levels and bilayer repetitions. The calculations have been performed using the TEY XMCD data (not shown) following the procedure described in Ref. [26].

<table>
<thead>
<tr>
<th></th>
<th>$x = 0$</th>
<th>$x = 0.15$</th>
<th>$x = 0.30$</th>
</tr>
</thead>
<tbody>
<tr>
<td>9_B</td>
<td>$-0.16(3)$</td>
<td>$-0.15(4)$</td>
<td>$-0.16(4)$</td>
</tr>
<tr>
<td>3_B</td>
<td>$-0.20(4)$</td>
<td>$-0.14(4)$</td>
<td>$-0.22(5)$</td>
</tr>
</tbody>
</table>
due to the nonresonant contributions of the other elements of the sample. In the following, we describe the procedure of this background subtraction for the example of the XMCD curves at the Cu-$L_{3,2}$ edges in the YBCO/LCMO superlattice.

The same procedure has been used for the analysis of the XLD curves and also for the XMCD and XLD curves of the LSCO/LCMO multilayers.

Panels (a) and (d) in Fig. 4 show the raw data for a series of XAS measurements, which have been performed with an applied field of 0.5 T at 2 K for circular polarization with positive and negative helicity. For each polarization, the measurement has been repeated three times. The TEY curves in panel (a) exhibit a noticeable intensity drift that is most likely caused by a weak charging effect of the sample. Panel (b) shows that this effect can be corrected for by normalizing the intensity with respect to the average value in the pre-edge region. Panels (d) and (e) show the corresponding correction procedure for the FY data where the intensity drift is significantly smaller. After this normalization the curves match very well in the regions before and after the edges and can now be directly compared.

The next step involves the subtraction of the background that arises from the nonresonant absorption due to the other elements in the sample. In a first approximation, the contribution of these remote absorption edges has been approximated with a linear function. Panels (b) and (d) show the result of the linear fit to the data in the pre-edge region. The TEY and FY curves after the subtraction of this linear background are displayed in panels (c) and (f). For the FY curve in panel (f), this yields a satisfactory result. For the TEY curve in panel (c) it is evident that this linear background subtraction is not as accurate. This is due to the very low probe depth of the TEY mode and the circumstance that the YBCO layer is buried below the topmost LCMO one. The Cu signal is therefore not much stronger than the background which is dominated by postedge features of the strong La-$M_{4,5}$ absorption edge near 850 eV. For the sum-rule analysis of the spin and orbital moments we have therefore performed an additional background subtraction that is outlined in Ref. [26].

Finally, for the Cu-$L_{3,2}$ edge FY and TEY curves shown in the main text, we have normalized the intensities with respect to the maximum of the peak at the $L_3$ edge. The $\mu_+$ and $\mu_-$ curves represent the average of the absorption curves for x-ray angular momentum antiparallel (positive helicity) and parallel (negative helicity) to the applied magnetic field, respectively, as measured for positive and negative field directions. This reduces the noise level and helps to remove instrumental artifacts. We note that the XTreme beamline allows one to change the polarization state of the x rays (via a modification of the undulator shift) without affecting the beam path to the sample and thus without modifying the offset or the dispersion of the energy scale [20].

APPENDIX B: WEIGHT OF THE PEAKS IN THE POLARIZATION-AVERAGED ABSORPTION

To relate the fitted intensity of the peaks with the fraction of the probed Cu atoms that contribute to each component in
the absorption, we have integrated the polarization-averaged absorption, \(2\mu_{ab} + \mu_c\), for each peak. In the averaged absorption, all the anisotropic contributions are canceled. Its area is directly proportional to the hole density in the Cu-3d band, which has been set to \(n_{3d} = 1\), and the number of the Cu atoms contributing to the particular transition [21]:

\[
A_{ab,i} + A_{c,i} = CN_i \left[ 2(2g_{3z^2-r^2} + 6g_{x^2-y^2}) + 8g_{3z^2-r^2} \right] = 12CN_i. \tag{B1}
\]

Here, \(A_{ab,i}\) is the fitted area of peak \(i\) for polarization in the direction \(\alpha\), \(N_i\) is the number of probed Cu atoms where the transition corresponding to peak \(i\) occurs, \(n_{3d}\) is the hole density in orbital \(j\), and \(C\) is an unknown proportionality constant. The different sensitivity to the \(\epsilon_p\) orbitals for different polarizations arises from the dependence of the transition probabilities on the anisotropy of the charge distribution [21]. The normalized weight of each peak in the polarization-averaged absorption is therefore directly related to the fraction of the probed Cu atoms that contribute to the transition:

\[
w_i = \frac{2A_{ab,i} + A_{c,i}}{\sum_j (2A_{ab,j} + A_{c,j})} = \frac{12CN_i}{12C \sum_j N_j} = \frac{N_i}{\sum_j N_j}, \tag{B2}
\]

where the summation runs over the peaks contributing to the absorption and thus \(\sum_j N_j\) corresponds to the total number of probed ions.

[22] Biskup et al. (unpublished).