EFFECTS OF USER’S TASTES ON PERSONALIZED RECOMMENDATION

JIAN-GUO LIU∗, TAO ZHOU†, BING-HONG WANG and YI-CHENG ZHANG

Research Center of Complex Systems Science
University of Shanghai for Science and Technology
Shanghai 200093, P. R. China

Department of Modern Physics
University of Science and Technology of China
Hefei 230026, P. R. China

Department of Physics, University of Fribourg
Fribourg CH-1700, Switzerland

∗liujg004@ustc.edu.cn
†zhutou@ustc.edu

QIANG GUO

School Business, University of Shanghai for Science and Technology
Shanghai 200093, P. R. China

In this paper, based on a weighted projection of the user-object bipartite network, we study the effects of user tastes on the mass-diffusion-based personalized recommendation algorithm, where a user’s tastes or interests are defined by the average degree of the objects he has collected. We argue that the initial recommendation power located on the objects should be determined by both of their degree and the user’s tastes. By introducing a tunable parameter, the user taste effects on the configuration of initial recommendation power distribution are investigated. The numerical results indicate that the presented algorithm could improve the accuracy, measured by the average ranking score. More importantly, we find that when the data is sparse, the algorithm should give more recommendation power to the objects whose degrees are close to the user’s tastes, while when the data becomes dense, it should assign more power on the objects whose degrees are significantly different from user’s tastes.

Keywords: Recommendation systems; bipartite network; network-based recommendation.

PACS Nos.: 89.75.Hc, 87.23.Ge, 05.70.Ln.

1. Introduction

With the rapid growth of the Internet and the World-Wide-Web, a huge amount of data and resource confront people with an information overload.1 There are
thousands of movies, millions of books, and billions of web pages on the web sites, and the amount of information is increasing more quickly than our personal processing abilities. This brings about massive amount of accessible information, which may result in a dilemma problem. It is hard for us to effectively filter out the pieces of information that are most appropriate for us. A landmark for information filtering is the use of search engine,\textsuperscript{2,3} by which user could find the relevant web pages by putting certain keywords. However, the search engine only returns the same results regardless of the user’s tastes and interests.

Thus far, the most promising way to efficiently filter out the information overload is to provide \textit{personalized recommendations}, which attempts to find out objects likely to be interesting to the target users by extracting the hidden information from the user’s historical selections or collections. Motivated by its significance for economy and society, the design of efficient recommendation algorithms has become a common focus for computer science, mathematics, marketing practices, management science and physics. Various kinds of algorithms have been proposed, such collaborative filtering (CF) approaches,\textsuperscript{4–8} content-based analyses,\textsuperscript{9,10} network-based algorithm,\textsuperscript{11–14} hybrid algorithms,\textsuperscript{16,17} and so on. For a review of current progress see Refs. 18 and 19 and the references therein.

Very recently, some physical dynamics, including mass diffusion (MD)\textsuperscript{13,14} and heat conduction (HC),\textsuperscript{11} have found their applications in personalized recommendations. These algorithms have been demonstrated to be of both high accuracy and low computational complexity.\textsuperscript{11–14} Since MD and HC algorithms could be implemented based on the user-object bipartite network, it is also called network-based algorithm. The network-based algorithm supposes that the objects one user has collected have the power to recommend new objects to the target user, which is coincidence with the definition reachability.\textsuperscript{15} In this paper, we introduce an improved MD algorithm with user-taste-dependent initial configuration. Compared with the uniform initial configuration, the prediction accuracy can be enhanced by using the user-taste-dependent configuration. More significantly, besides the prediction accuracy, we find that the data sparsity is an important factor affecting the algorithm performance. When the sparsity of the user-object bipartite network is small, in other words, there are few edges between the users and objects, the algorithm should pay more attention on the user’s habits and tastes, while when the number of edges in the bipartite network is large, the algorithm should give more recommendation power on the objects whose degrees are significantly different with user’s habits. Numerical simulations show that the improved algorithm has higher accuracy and can provide more diverse and less popular recommendations.

2. Mass-Diffusion-Based Personal Recommendation

In a recommender system, each user has voted or collected some objects, the system could be described by a bipartite network, in which there are two kind of nodes, users and objects, the user’s historical collection or selection behaviors could be
well demonstrated by the edges connecting the users and objects. Formally, denote the object set as \( O = \{o_1, o_2, \ldots, o_m\} \) and the user set as \( U = \{u_1, u_2, \ldots, u_n\} \), the system can be fully described by a bipartite network with \( m + n \) nodes, where there is an edge between a user and object if and only if this object is collected by the user. The bipartite network could be described by an adjacent matrix \( A = \{a_{ij}\} \in \mathbb{R}^{m,n} \), where \( a_{ij} = 1 \) if \( o_i \) is collected by \( u_j \), and \( a_{ij} = 0 \) otherwise. In MD algorithm, an object-object similarity network \( W = \{w_{\alpha\beta}\}_{m,m} \) is constructed first, where each node represents an object and two objects are connected if they have been collected simultaneously by at least one user. Then, to a target user, an amount of recommendation power is set on each object he has collected, and the proportion of the resource \( w_{\alpha\beta} \) would like to distribute from \( o_{\beta} \) to \( o_{\alpha} \). In MD, a reasonable assumption is that the objects that users have collected are what they like, and the objects a target user has collected would be regarded as the initial mass source, then the activated objects redistribute the mass to the users who have collected them before, with users receiving a level of mass equal to the mean amount possessed by their neighboring objects, and objects then receiving back the mean of their neighboring users’s mass levels. Due to the sparsity of real data sets, these “physical” descriptions of the algorithm turn out to be more computationally efficient in practice than constructing and using the object similarity matrix \( W \), and MD algorithm could be implemented in three steps on the user-object bipartite network, which is shown in Figs. 1(a)–1(c).

Lind et al. presented a cycle measurement to investigate the clustering property in bipartite network.\(^{20,21}\) According to the algorithm description and the cycle definition, the object similarity of the mass-diffusion-based algorithm can be expressed

![Fig. 1. Illustration of the network-based algorithm. The network-based algorithm could be applied in the following way. (a) The objects collected by the target user are activated. (b) The heat is diffused from the activated objects to the users who have collected them. (c) Then it is diffused back from the users to the objects.](http://doc.rero.ch)
as,
\[ w_{\alpha\beta} = \frac{1}{k(o_{\beta})} \sum_{l=1}^{n} a_{\alpha l} a_{\beta l}, \]  
(1)

where \( k(o_{\beta}) = \sum_{i=1}^{n} a_{\beta i} \) and \( k(u_i) = \sum_{i=1}^{m} a_{il} \) denote the degrees of object \( o_{\beta} \) and user \( u_i \), respectively. For a target user, in the simplest case, the initial resource vector \( f = \{ f_1, f_2, \ldots, f_m \}^T \) can be set as
\[ f_j = a_{ji}. \]  
(2)

In other words, only the objects user \( u_i \) has collected are set unit resource. After the mass-diffusion-process demonstrated in Fig. 1, the final resource vector is
\[ \hat{f} = Wf. \]  
(3)

Sorting the vector \( \hat{f} \) in descending order according to value of \( \hat{f}_j \), the objects obtained the highest values are recommended to the target user.

3. Improved Algorithm by Considering the User’s Taste Effects

In the standard MD algorithm, for any user \( u_i \), all of the collected objects are assigned the same recommendation power. Although it already has a good algorithmic accuracy, this uniform configuration may be oversimplified, and did not consider the effects of user’s tastes. In this paper, the user’s taste is defined by the average object degree he has collected. The objects whose degrees are close to the user’s taste should be assigned more recommendation power. We also notice that most of the user’s tastes are less than 100, while the degrees of the popular objects are close to 300. If the recommendation power is assigned according to the distance between the object degree and the user’s taste, it will give more power on the popular objects and weaken the unpopular object effects. In order to balance the objects whose degrees are larger or less than the user’s tastes, we present a more complicated distribution of initial resource according to the following way.
\[ f_{\alpha}^i = a_{\alpha i} I_{\alpha i}, \]  
(4)

where \( I_{\alpha i} \) is defined as follows
\[ I_{\alpha i} = \begin{cases} \left( \frac{k(o_{\alpha})}{k(u_i)} \right)^{\beta} & k(o_{\alpha}) \geq \bar{k}(u_i) \\ \left( \frac{\bar{k}(u_i)}{k(o_{\alpha})} \right)^{\beta} & k(o_{\alpha}) < \bar{k}(u_i) \end{cases} \]  
(5)

where \( \bar{k}(u_i) \) denote the average degree of user \( u_i \)’s collected objects, and \( \beta \) is a tunable parameter. Compared with the uniform case, \( \beta = 0 \), a positive \( \beta \) strengthens the influence of the objects whose degrees are larger or less than \( \bar{k}(u_i) \), while a negative \( \beta \) strengthen the influence of the objects whose degrees are close to \( \bar{k}(u_i) \).
4. Numerical Results

A benchmark dataset, namely MovieLens, is used to test the improved algorithm. The MovieLens data is a randomly-selected subset of the huge data, which consists of 1682 movies (objects) and 943 users. The users vote movies by discrete ratings from one to five. We applied a coarse-graining method: A movie is set to be collected by a user only if the giving rating is larger than 2. The original data contains $10^5$ ratings, 85.25% of which are $\geq 3$, that is, the user-object (user-movie) bipartite network after the coarse graining contains 85250 edges. We randomly divide this data set into two parts: one is the training set, treated as known information, and the other is the probe, whose information is not allowed to be used for prediction. We use a parameter $p$ to control the data density, that is, $p\%$ of the ratings are put into the probe set, and the remains compose the training set.

A good recommender method should rank preferable objects to math the user’s tastes. Therefore, the collected objects in the probe set should be set at the top level of the recommendation lists. The average ranking score is adopted to measure the accuracy. It could be defined as follows. For a target user $u_i$, if the entry $u_i-o_j$ is in the probe set, we measure the position of $o_j$ in the ordered list. For example, if there are $L_i = 10$ uncollected objects for $u_i$, and $o_j$ is the second one from the top, we say the position of $o_j$ is 2/10, denoted by $r_{ij} = 0.2$. A good algorithm is expected to give high recommendations to them, thus leading to small $r_{ij}$. Therefore, the mean value of the position $\langle r \rangle$ can be used to evaluate the algorithmic accuracy: the smaller the average ranking score, the higher the algorithmic accuracy, and vice versa. The average degree of all recommended objects, $\langle k \rangle$, and the mean value of Hamming distance, $S$, are taken into account to evaluate the popularity and diversity. The smaller average degree, corresponding to the unpopular objects, are preferred since those small-degree objects are hard to be found by users themselves. The diversity can be quantified by the average Hamming distance, $S = \langle H_{ij} \rangle$, where $H_{ij} = 1 - Q_{ij}/L$, $L$ is the length of recommendation list and $Q_{ij}$ is the overlapped number of objects in $u_i$ and $u_j$’s recommendation lists. The largest $S = 1$ indicates the recommendations to all of the users are totally different, while the smallest $S = 0$ means all of recommendations are exactly the same.

Implementing the improved algorithm on the MovieLens data, the accuracy, popularity and diversity are investigated. Figure 2 reports the algorithmic accuracy as a function of $\beta$ to different $p$, from which one can find that the curves obtained by the improved algorithm has clear minimums, which strongly support the above discussion. Compared with the routine case ($\beta = 0$), the average ranking score can be reduced 5.6% at the optimal case when $p = 10$. Numerical results on different percentage of probe sets show that the optimal parameter $\beta_{opt}$ decreases with the increase of $p$. Figure 3 reports the relation between the optimal $\beta_{opt}$, the corresponding average ranking scores $\langle r \rangle_{opt}$ and the sparsity of the training sets. One can see from Fig. 3 that the optimal $\langle r \rangle_{opt}$ is negatively correlated with the data sparsity, where the sparsity is defined as $E/(m \times n)$, and $E$ is the number of
edges in the user-object bipartite network, more interestingly, the optimal parameter $\beta_{opt}$ is positively correlated with the sparsity. The reason may lie in the fact that when the users have not collected too much objects, their tastes are easy to be distinguished, therefore, the objects whose degrees are close to $\bar{k}(u_i)$ should be
Fig. 4. When the recommendation list $L = 10$, $\langle k \rangle$ and $S$ vs $\beta$ of $p = 10, 20, 30$ and $40$. All the data points are averaged over ten independent runs with different data-set divisions.

assigned more recommendation power. As the number of user’s collected objects increases, user’s tastes become diversity, therefore, it is hard to catch the user’s interests and habits. Under these circumstances, the users are more interesting to the objects different from his historical collects which could bring him/her fresh information. Besides accuracy, the popularity and diversity are also investigated. Figure 4 reports the average degree and diversity of all recommended movies as a function of $\beta$ to different $p$ when the recommendation lists $L = 10$, from which one can find that although the average object degrees scarcely change, the diversity is increased at the optimal $\beta_{opt}$.

5. Conclusion and Discussion

In this paper, the effects of user’s tastes on MD recommendation algorithm are investigated, where the user’s tastes are defined by the average object degree he/she has collected. By introducing a free parameter $\beta$, an improved algorithm by regulating the initial configuration of resource is presented. Numerical results indicate that when the data set is sparse, it is easy to distinguish the user’s tastes and the objects whose degrees are close to the user’s tastes should be assigned more recommendation power, while as the data set becomes dense, the objects whose degree are far from the user’s tastes should be emphasized. Besides the average ranking score, the popularity and personalization of recommended objects are also taken into account. The results show that the improved algorithm outperforms the standard MD algorithm in both accuracy and personalization.

In the improved algorithm, we only give a kind of user taste definition, however, there are several other ways to define the user’s tastes, such as time-dependent
behavior, variance of the user collected object degrees, and so on. We believe MD algorithm could be further improved by catching the user’s current tastes. Instead of calculating all the elements in $W$, one can implement the current algorithm by directly diffusing the resource of each user. Ignoring the degree-degree correlation in user-object relations, the algorithmic complexity is $O(m\langle k_u \rangle \langle k_o \rangle)$, where $\langle k_u \rangle$ and $\langle k_o \rangle$ denote the average degrees of users and objects. Theoretical physics provides us with some beautiful and powerful tools in dealing with this long-standing challenge in modern information science: how to do a personal recommendation. The presented algorithm could also be used to find the relevant reviewers for the scientific papers or funding applications, and the link prediction in social and biological networks. We believe the current work can enlighten readers in this promising direction.

Acknowledgment

This work is partially supported by the National Basic Research Program of China (No. 2006CB705500), the National Natural Science Foundation of China (Nos. 60744003, 10635040, 10472116, 10905052, 70901010), the Swiss National Science Foundation (Project 205120–113842), and Shanghai Leading Discipline Project (Grant No. S30501).

References